

---

# **Program Validation by Symbolic and Reverse Execution**

Jooyong Lee

BRICS

Department of Computer Science

University of Aarhus

# Computer Programs

Introduction

● **Computer Programs**

- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

Reverse Execution

Program Validation by  
Symbolic Execution

Concluding Remarks

**Programs are everywhere.**

# Computer Programs

## Introduction

### ● Computer Programs

- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



# Computer Programs

## Introduction

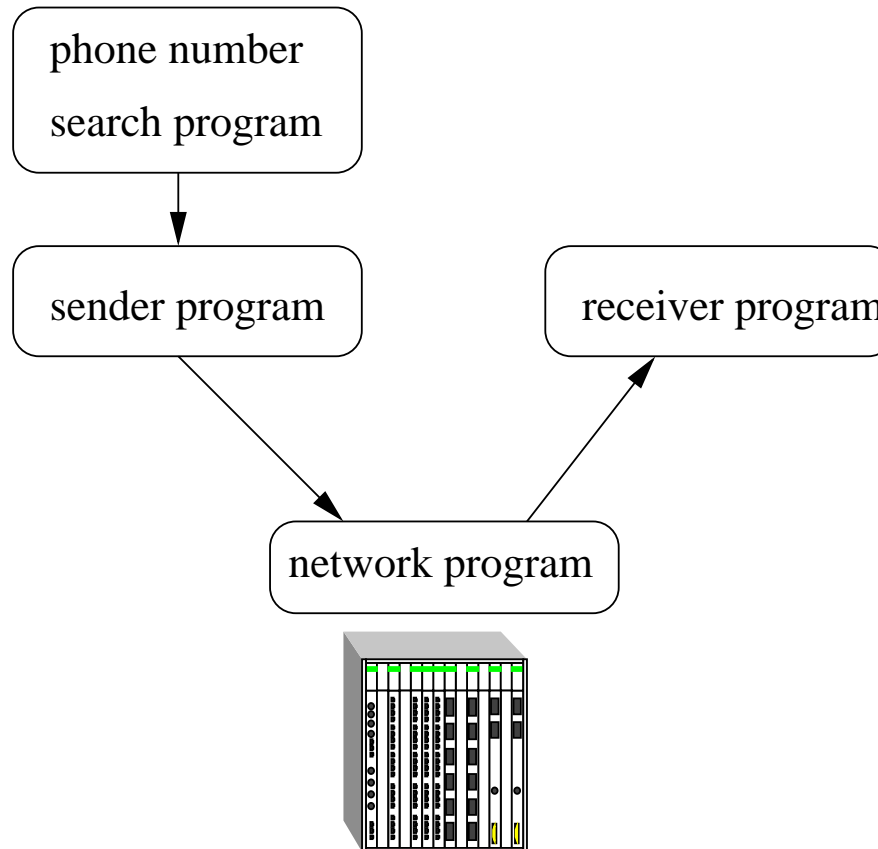
### ● Computer Programs

- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



# Computer Programs

Introduction

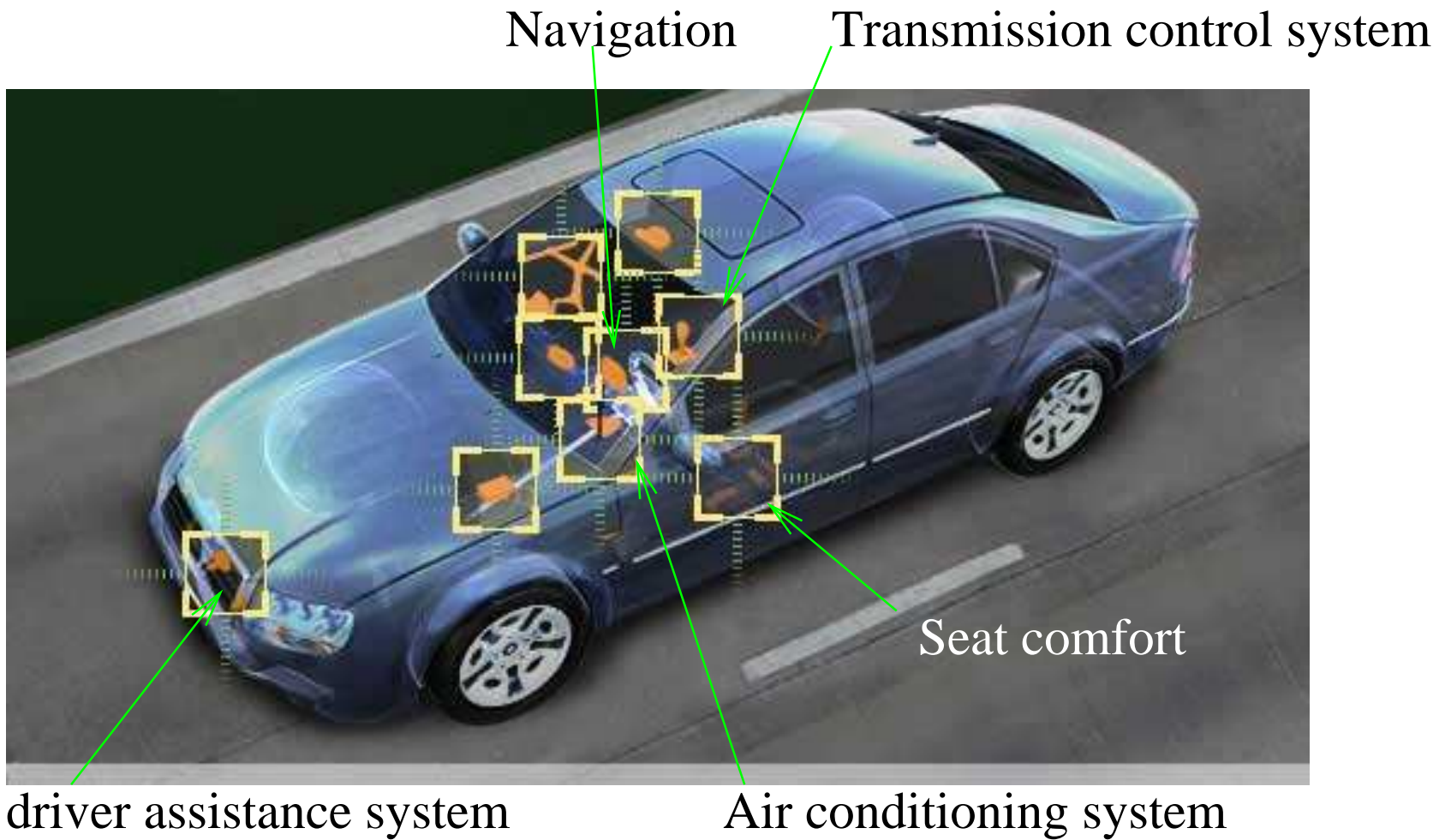
● Computer Programs

- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

Reverse Execution

Program Validation by  
Symbolic Execution

Concluding Remarks



# Computer Programs

Introduction

● Computer Programs

- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

Reverse Execution

Program Validation by  
Symbolic Execution

Concluding Remarks



- Ariane 5: an unmanned rocket
- Everything is controlled by programs.



# Computer Programs

## Introduction

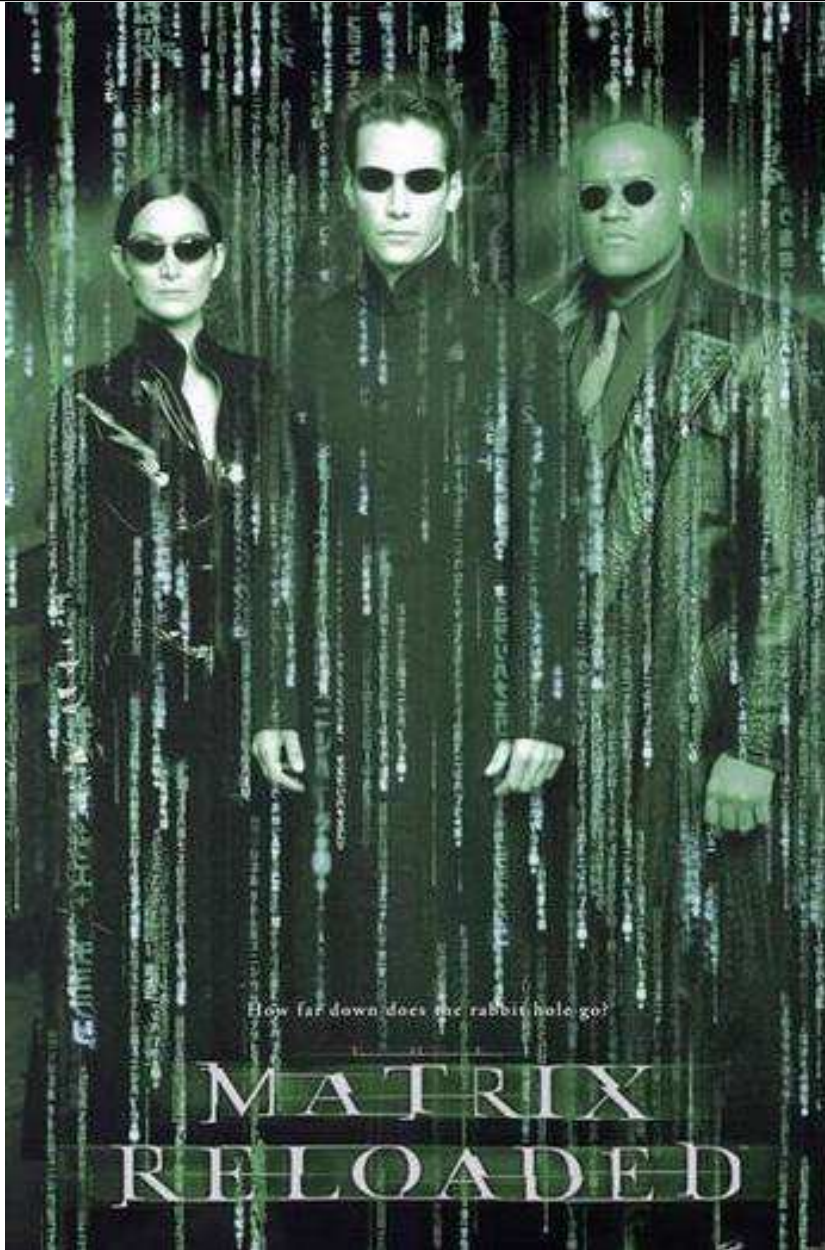
### ● Computer Programs

- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



Who knows?

We may be living our lives as  
programs in the Matrix.

# Program Errors (aka 'Bugs')

---

## Introduction

- Computer Programs
- **Program Errors (aka 'Bugs')**
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

---

## Reverse Execution

Program Validation by  
Symbolic Execution

---

Concluding Remarks

---

**Bugs are everywhere.**



A problem has been detected and windows has been shut down to prevent damage to your computer.

The problem seems to be caused by the following file: SPCMDCON.SYS

PAGE\_FAULT\_IN\_NONPAGED\_AREA

If this is the first time you've seen this Stop error screen, restart your computer. If this screen appears again, follow these steps:

Check to make sure any new hardware or software is properly installed. If this is a new installation, ask your hardware or software manufacturer for any Windows updates you might need.

If problems continue, disable or remove any newly installed hardware or software. Disable BIOS memory options such as caching or shadowing. If you need to use Safe Mode to remove or disable components, restart your computer, press F8 to select Advanced Startup Options, and then select Safe Mode.

Technical information:

\*\*\* STOP: 0x00000050 (0xFD3094C2,0x00000001,0xFBFE7617,0x00000000)

\*\*\* SPCMDCON.SYS - Address FBFE7617 base at FBFE5000, DateStamp 3d6dd67c

# Program Errors (aka 'Bugs')

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



Is it really OK?

# Program Errors (aka 'Bugs')

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



- Recall of Chrysler Pacifica in 2006
- Summary: ON CERTAIN PASSENGER VEHICLES, THE FUEL PUMP MODULE AND THE POWER TRAIN CONTROL MODULE SOFTWARE MAY ALLOW THE ENGINE TO STALL UNDER CERTAIN OPERATING CONDITIONS.
- Consequence: THIS COULD CAUSE A CRASH TO OCCUR WITHOUT PRIOR WARNING.

# Program Errors (aka 'Bugs')

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



- The Ariane 5 rocket exploded 40 seconds after its launch due to a **program bug** in 1996.

# Topic of My Thesis

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- **Topic of My Thesis**
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



**CHECKING FOR BUGS**

**&**

**LOCATING BUGS**

**in programs**

# Topic of My Thesis

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks



## PROGRAM VALIDATION



# Program Life-cycle



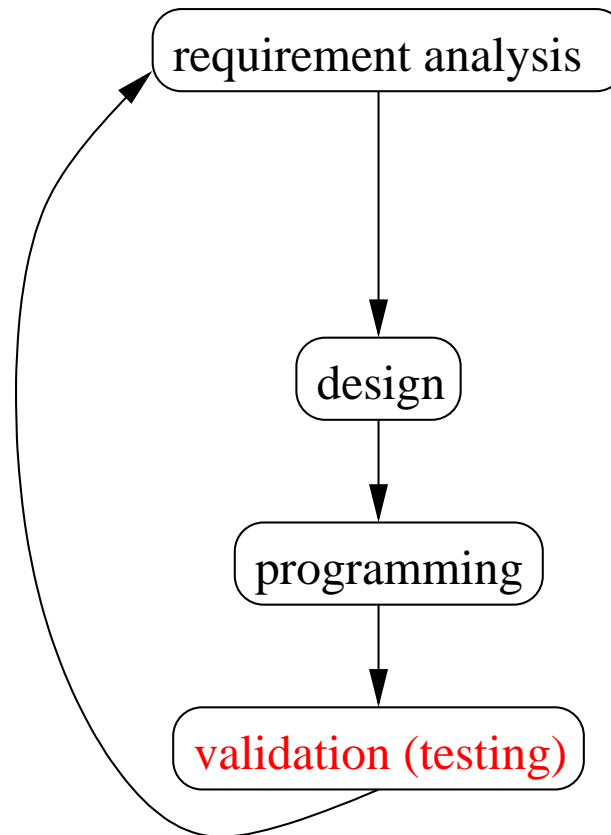
## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

Program Validation by  
Symbolic Execution

## Concluding Remarks



# Program Life-cycle

---

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- **Program Life-cycle**
- My Thesis (What)
- My Thesis (How)
- Plan

---

## Reverse Execution

---

Program Validation by  
Symbolic Execution

---

---

Concluding Remarks

---



# Program Life-cycle



## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

Program Validation by  
Symbolic Execution

## Concluding Remarks

requirement analysis

design

programming

validation (testing)

What kind of food?  
How many guests?  
Dietetic requirements

recipe

cooking

tasting

# Program Life-cycle

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

Program Validation by  
Symbolic Execution

## Concluding Remarks



requirement analysis

What kind of food?  
How many guests?  
Dietetic requirements

design

recipe

programming

cooking

validation (testing)

tasting



# My Thesis (What)

## Program Validation

### Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

### Reverse Execution

Program Validation by  
Symbolic Execution

### Concluding Remarks

# My Thesis (How)

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)
- Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks

## Program Validation by Symbolic and Reverse Execution



- Symbolic Execution
  - ◆ Checking for Bugs



- Reverse Execution
  - ◆ Locating Bugs



# Plan

## Introduction

- Computer Programs
- Program Errors (aka 'Bugs')
- Topic of My Thesis
- Program Life-cycle
- My Thesis (What)
- My Thesis (How)

## ● Plan

## Reverse Execution

## Program Validation by Symbolic Execution

## Concluding Remarks

## 1. Introduction

## 2. Reverse Execution

- (a) What is it?
- (b) Existing Work?
- (c) Problem?
- (d) Contribution: Dynamic Reverse Code Generation
- (e) Soundness
- (f) Case Study

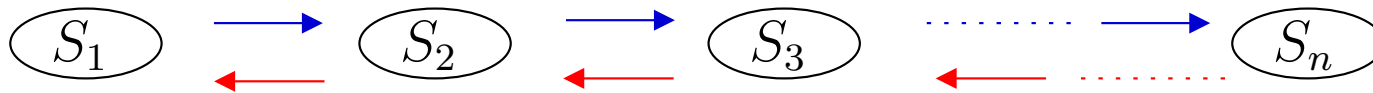
## 3. Symbolic Execution

- (a) What is it?
- (b) Existing Work?
- (c) Contribution: Bounded Lazier Initialization
- (d) Soundness and Completeness

## 4. Concluding Remarks

# What?

- What is reverse execution?
  - ◆ A series of **state restorations**
- What is execution?
  - ◆ A series of **state changes**



Introduction

Reverse Execution

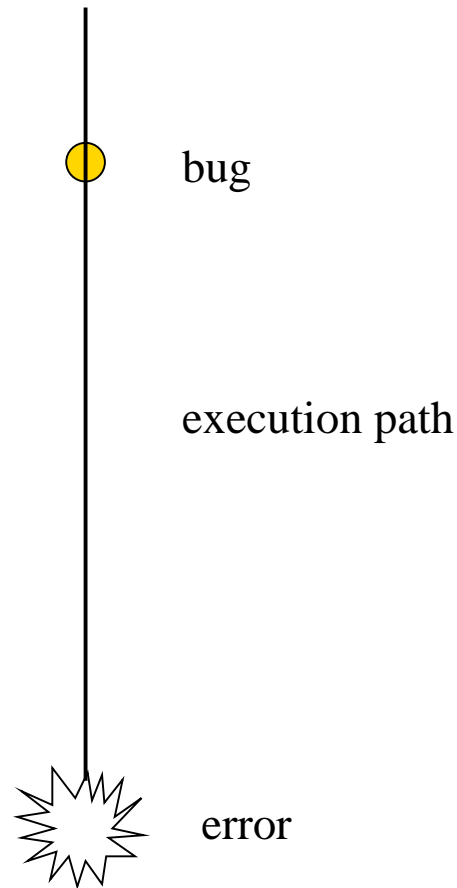
● What?

- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Locating a Bug

- Butterfly Effect: Something as small as the flutter of a butterfly's wings can ultimately cause a typhoon halfway around the world.



Introduction

Reverse Execution

● What?

● Locating a Bug

● Locating a Bug by Iterative Execution

● Locating a Bug by Reverse Execution

● Reverse-Execution Methods

● Loop Example

● Reverse Execution by State-Saving

● Reverse Execution by Checkpointing

● Reverse Execution by Checkpointing

● Reverse Execution by Reverse Code

● Reverse Code Generation

● Static Reverse Code

Generation

● Multi-threaded Programs

● Dynamic Reverse Code

Generation

● Static vs. Dynamic Reverse Code Generation

● Dynamic Reverse Code

Generation

● Multiple Variables

● Combination

● Soundness

● Bounded Buffer Example

(Chapter 8)

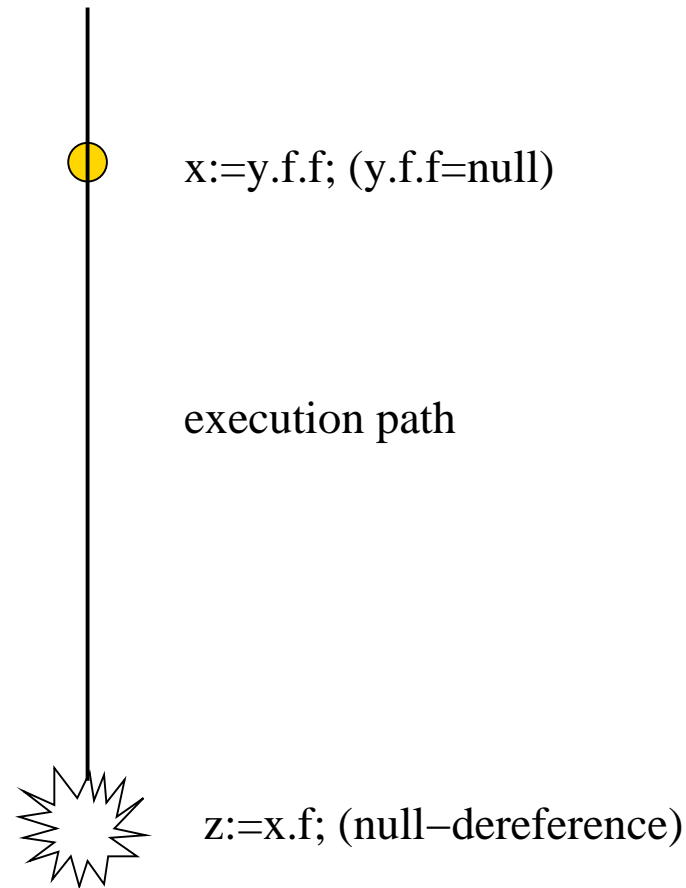
Programming with Monads, 2007

Symbolic Execution

BRICS - p. 12/49

# Locating a Bug

- Butterfly Effect: Something as small as the flutter of a butterfly's wings can ultimately cause a typhoon halfway around the world.



Introduction

Reverse Execution

● What?

● Locating a Bug

● Locating a Bug by Iterative Execution

● Locating a Bug by Reverse Execution

● Reverse-Execution Methods

● Loop Example

● Reverse Execution by State-Saving

● Reverse Execution by Checkpointing

● Reverse Execution by Checkpointing

● Reverse Execution by Reverse Code

● Reverse Code Generation

● Static Reverse Code Generation

● Multi-threaded Programs

● Dynamic Reverse Code Generation

● Static vs. Dynamic Reverse Code Generation

● Dynamic Reverse Code Generation

● Multiple Variables

● Combination

● Soundness

● Bounded Buffer Example

(Chapter 8)

Program Verification, 2007

Symbolic Execution

BRICS - p. 12/49

# Locating a Bug by Iterative Execution

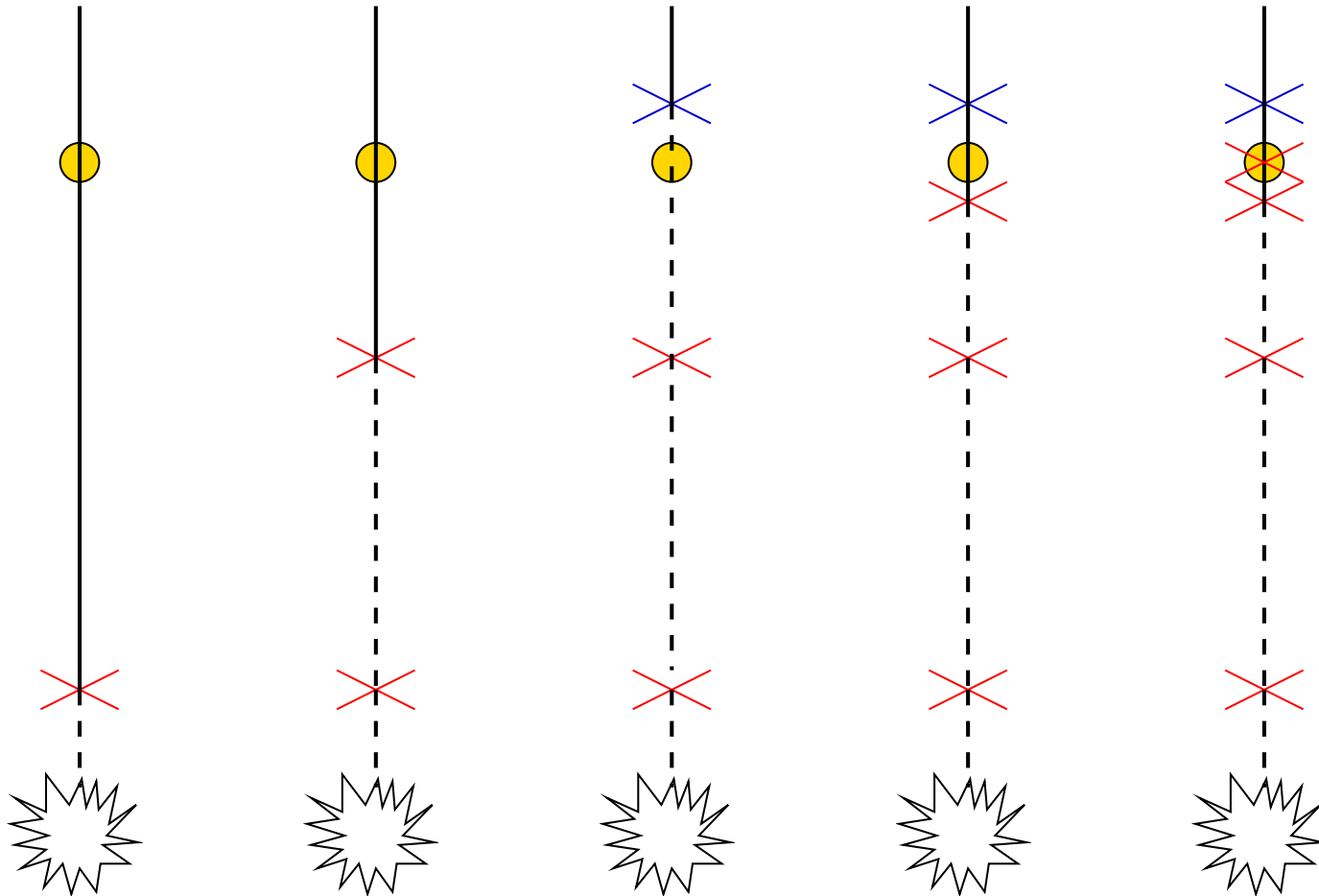
## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution

## Locating a Bug by Reverse Execution

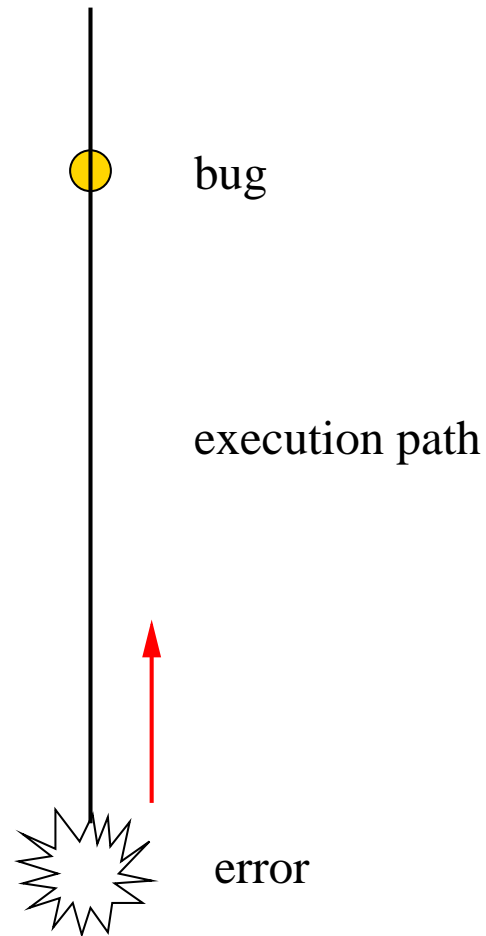
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example



(Chapter 8)

# Locating a Bug by Reverse Execution

- As an alternative, reverse execution has been suggested
- Functionally similar to undo in text editors



## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



# Reverse-Execution Methods

Introduction

Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- **Reverse-Execution Methods**
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

Programming Language Theory, 2007  
Symbolic Execution

In the literature:

- State-Saving
- Checkpointing
- Reverse Code

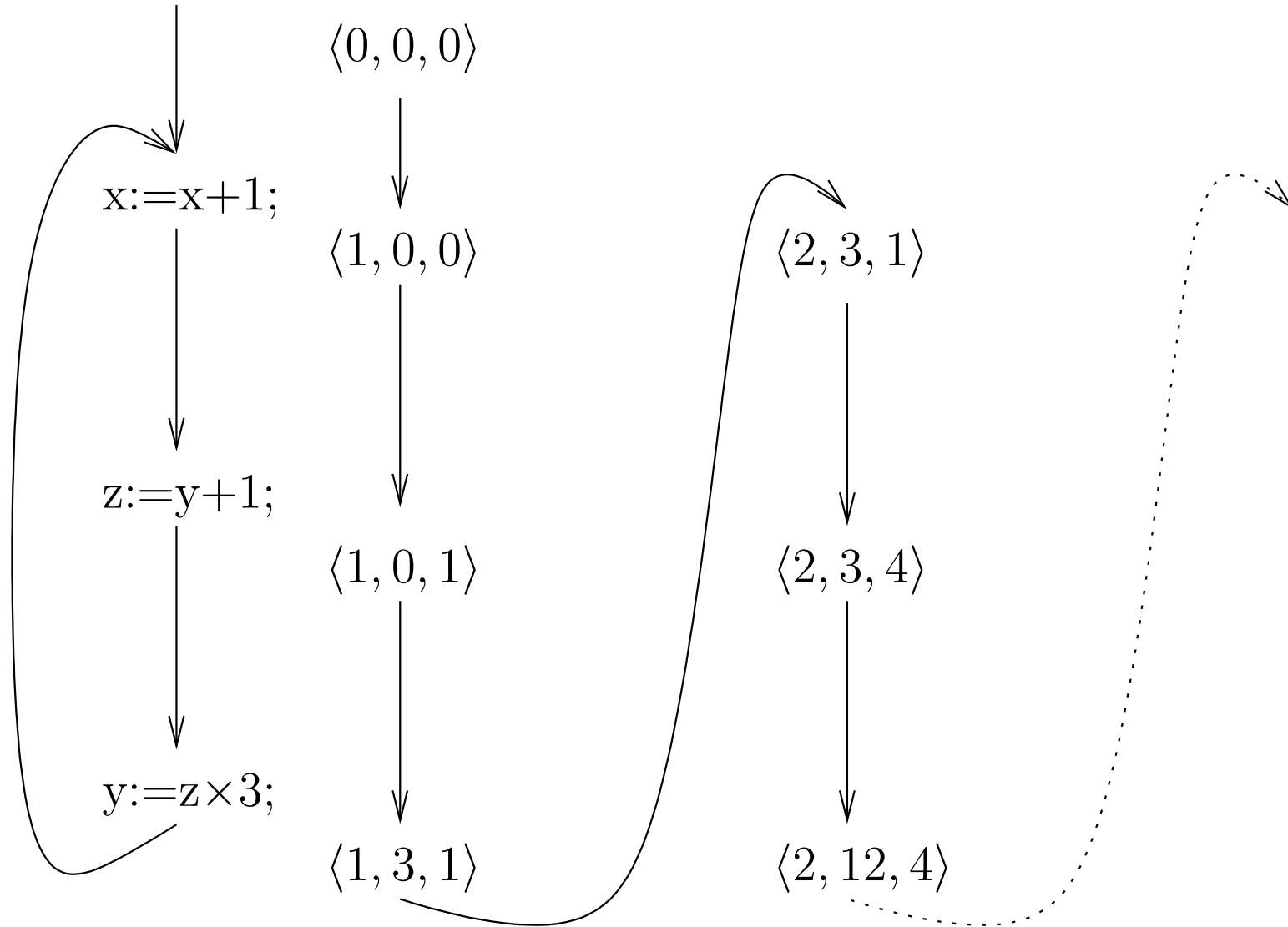
# Loop Example

Introduction

Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- **Loop Example**
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

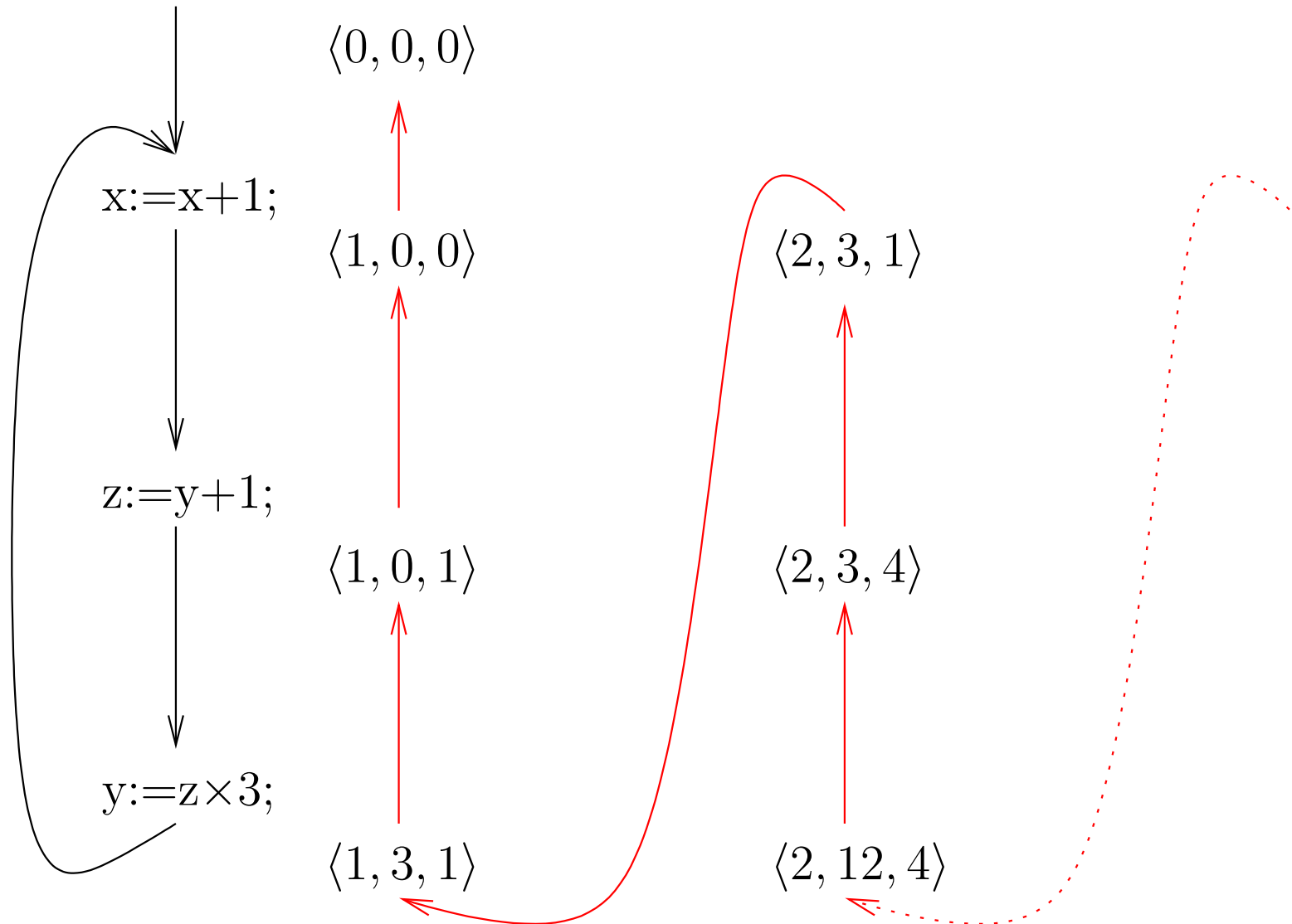


# Loop Example

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- **Loop Example**
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

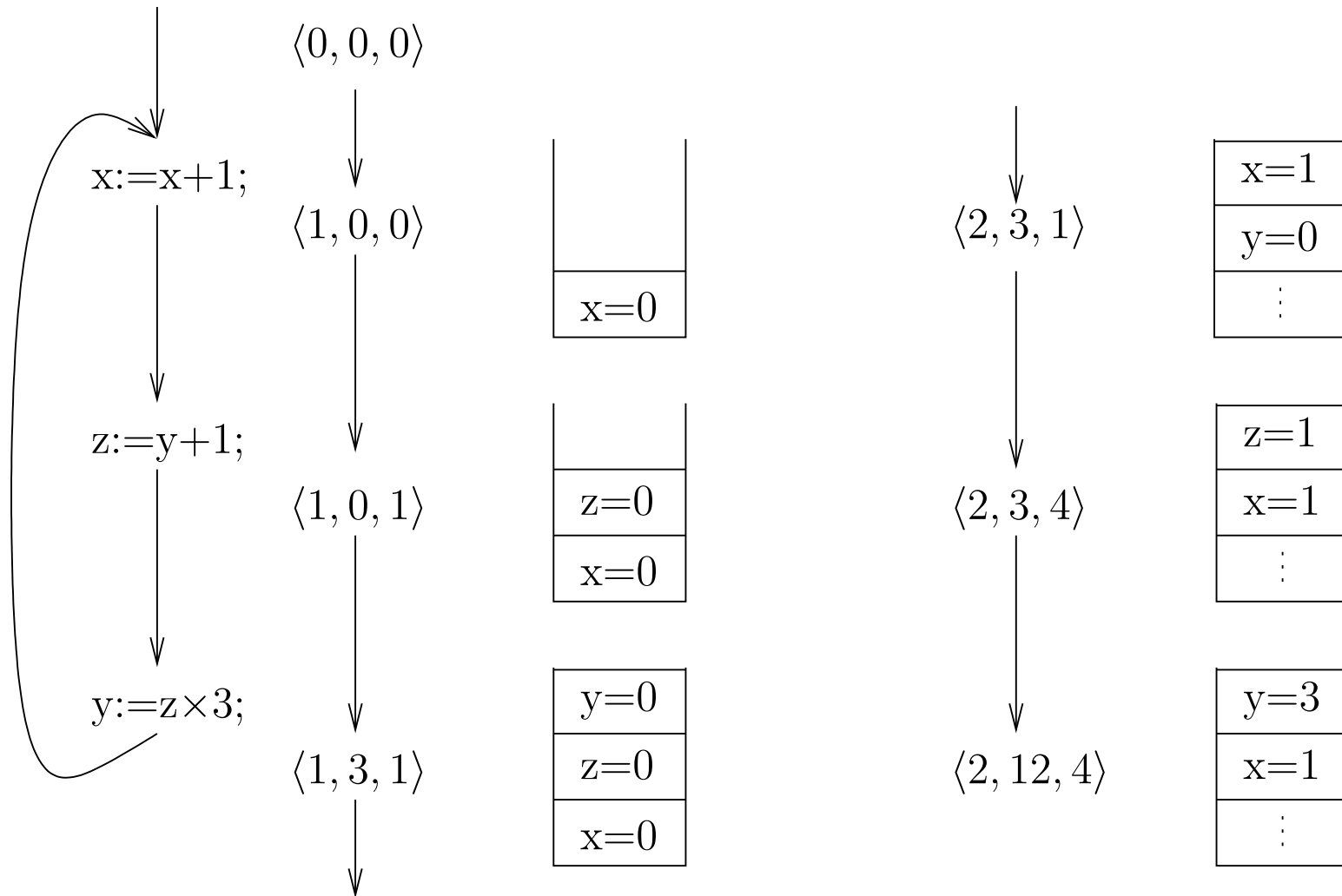


# Reverse Execution by State-Saving

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example



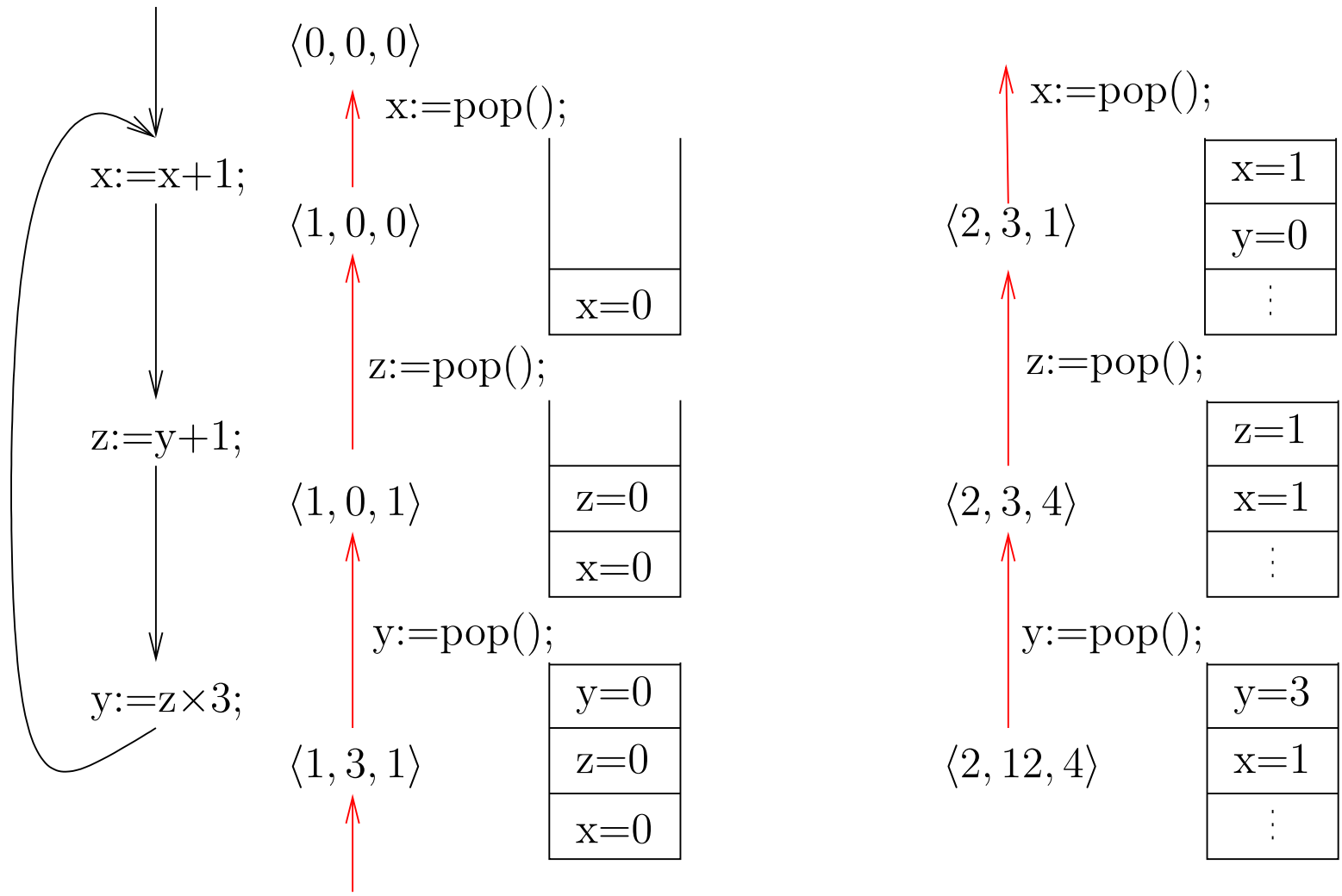
(Chapter 8)

# Reverse Execution by State-Saving

## Introduction

## Reverse Execution

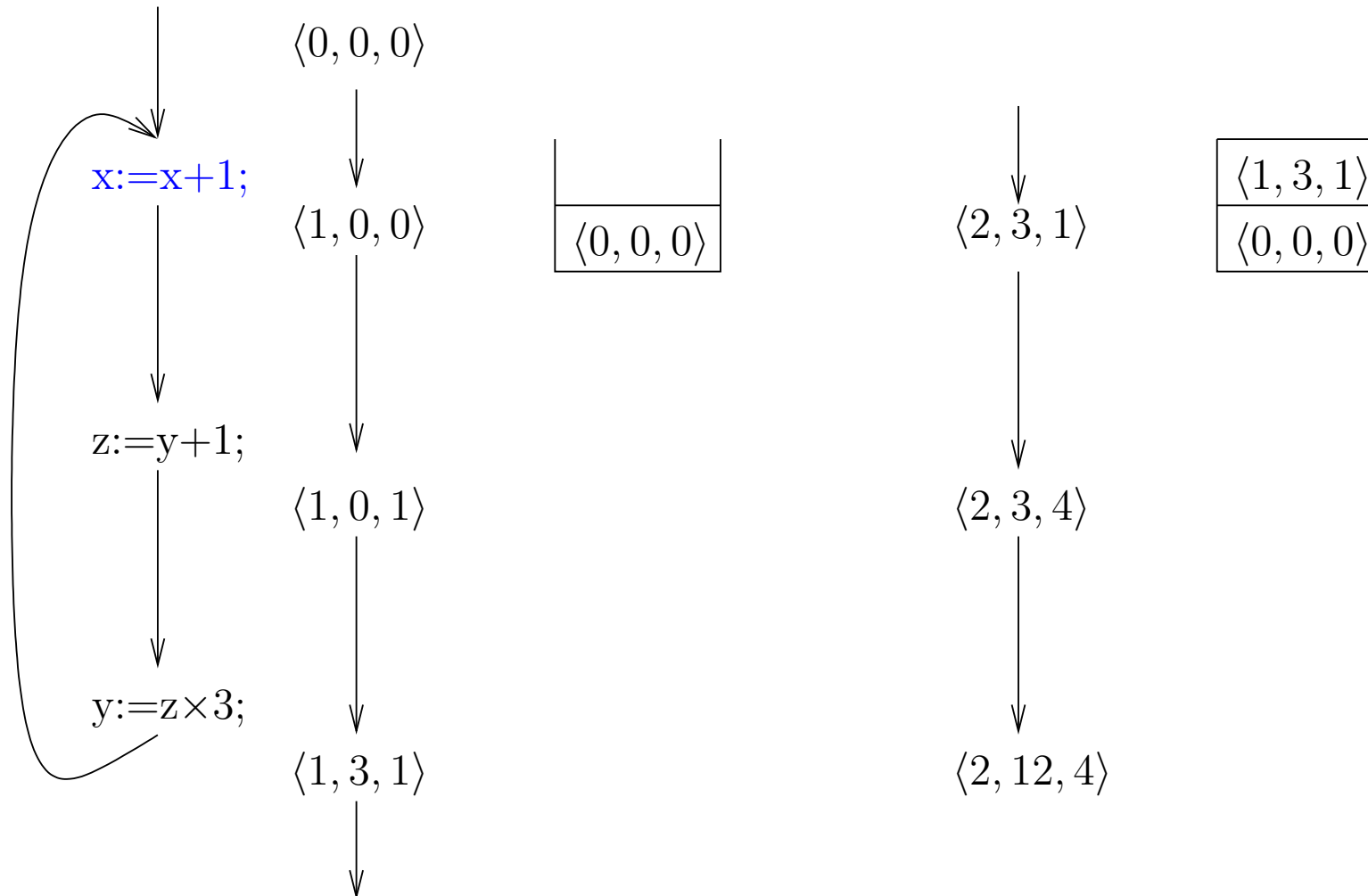
- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example



(Chapter 8)

# Reverse Execution by Checkpointing

## ■ Periodic state-saving



Introduction

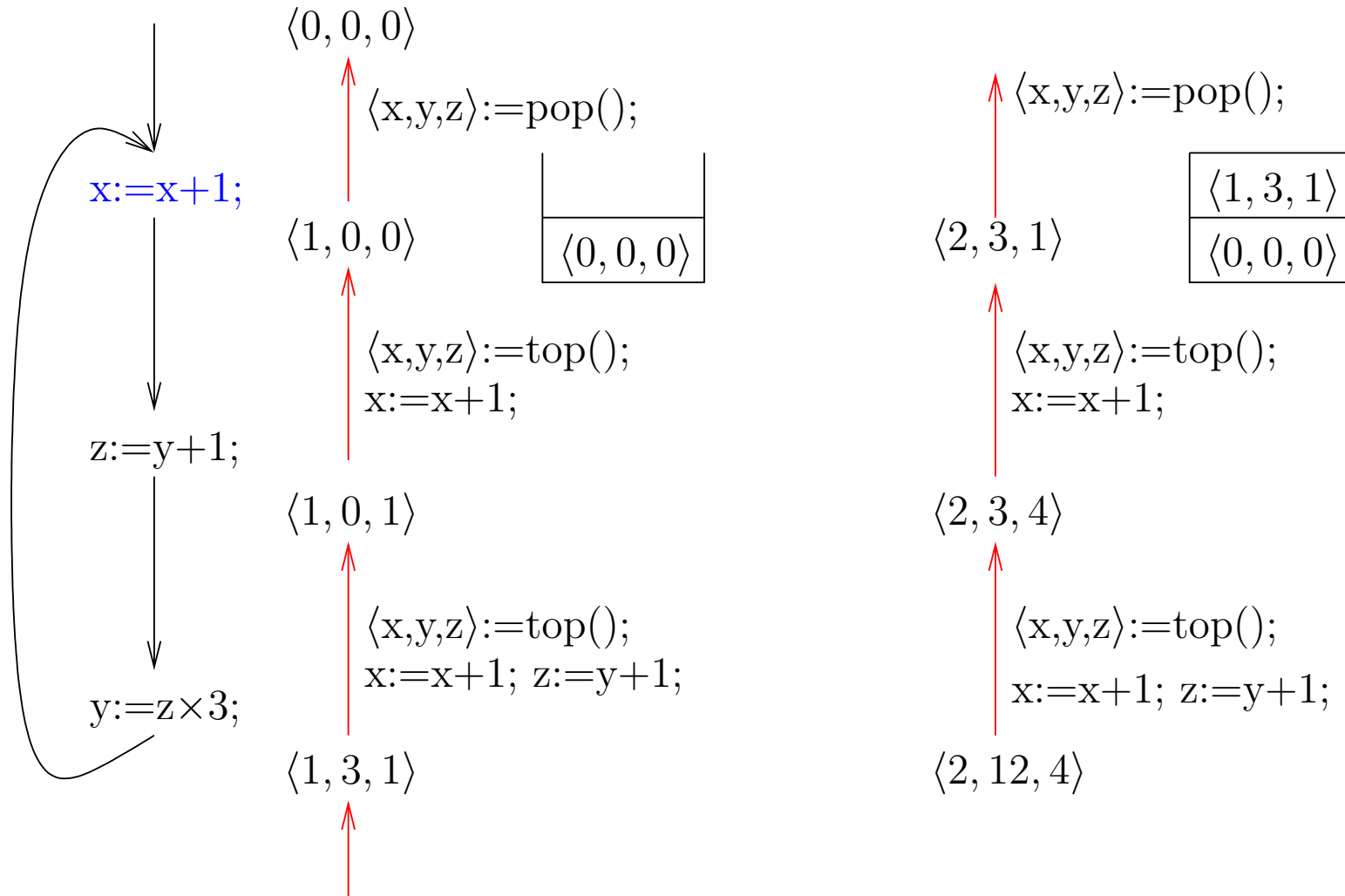
Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Reverse Execution by Checkpointing

## ■ Periodic state-saving



Introduction

Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- **Reverse Execution by Checkpointing**
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Reverse Execution by Checkpointing

- Periodic state-saving
- It consumes fewer stack elements than state-saving if...
- State-saving and checkpointing depend heavily on the use of the stack
- The stack is usually allocated in the memory of a computer

Introduction

Reverse Execution

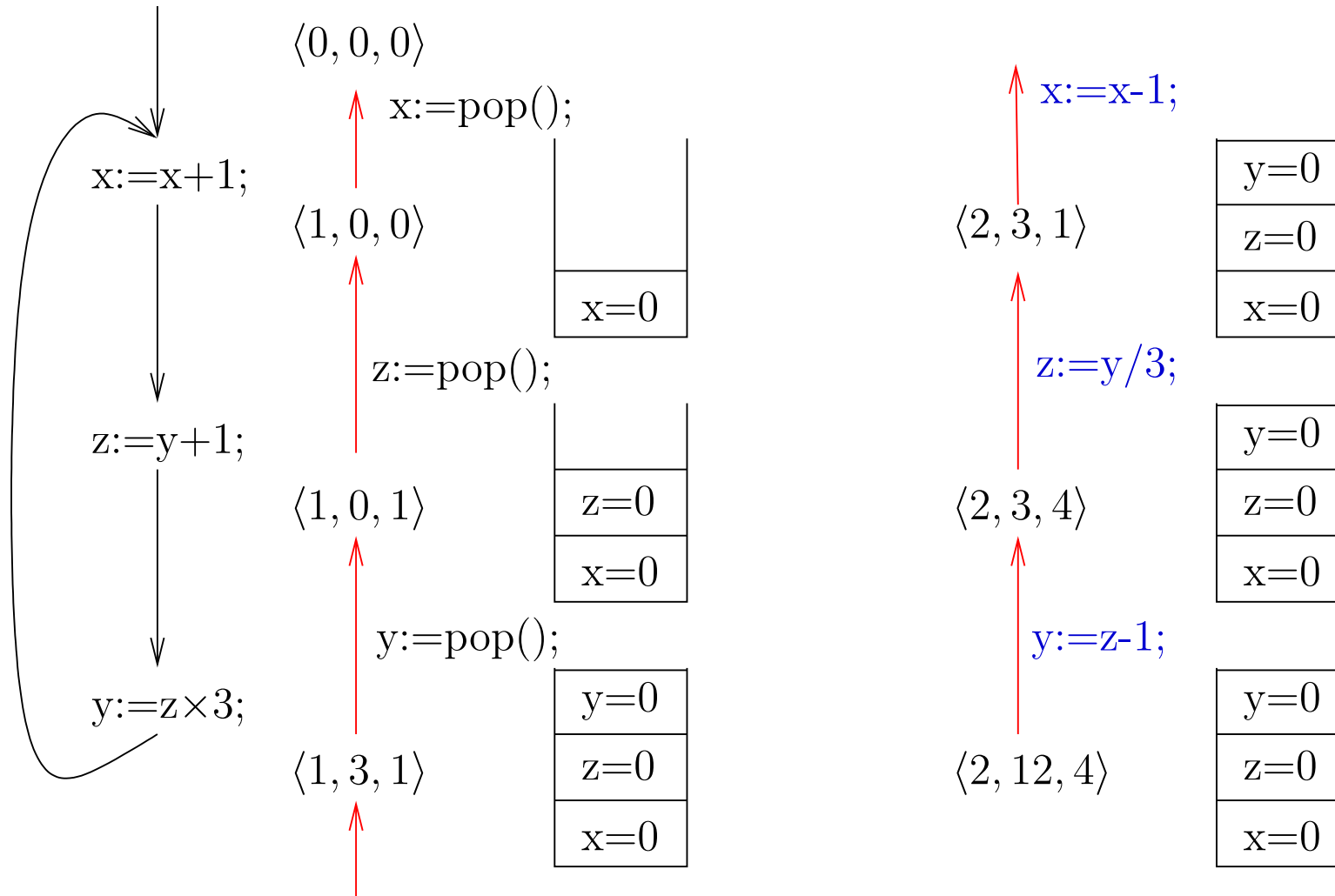
- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



# Reverse Execution by Reverse Code

## ■ Reverse code alleviates the situation



Introduction

Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Reverse Code Generation

Introduction

Reverse Execution

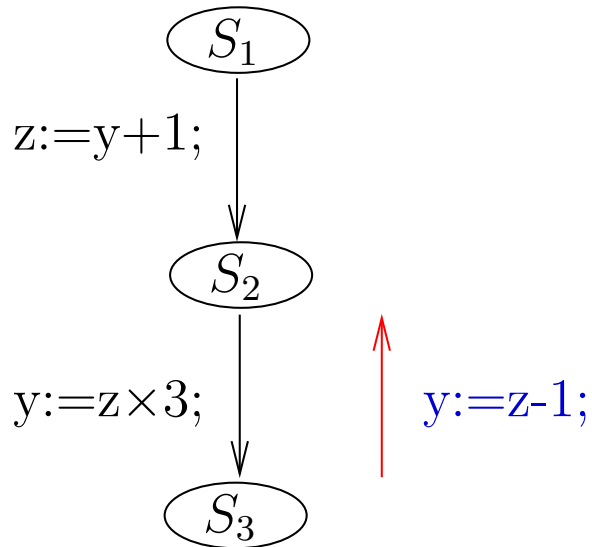
- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code

● Reverse Code Generation

- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

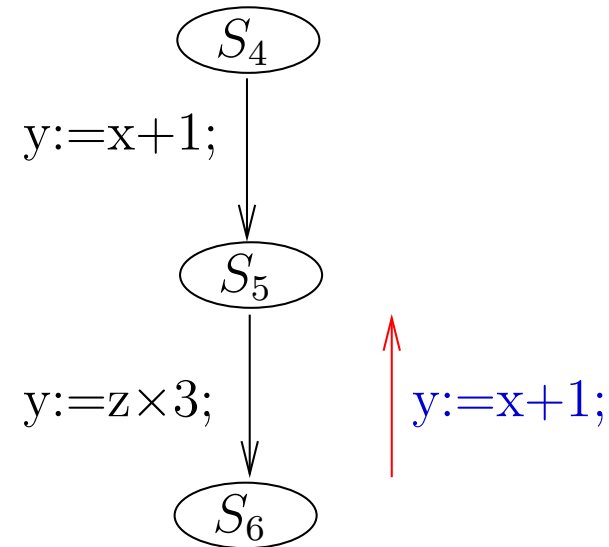
(Chapter 8)

## ■ Extraction-from-use



- $y$  was used in  $z:=y+1;$ .
- $z = (\lambda t.t + 1)(y)$
- $y = (\lambda t.t + 1)^{-1}(z)$
- $(\lambda t.t + 1)^{-1} = (\lambda t.t - 1)$
- $y = (\lambda t.t - 1)(z)$
- $y := z - 1;$ .

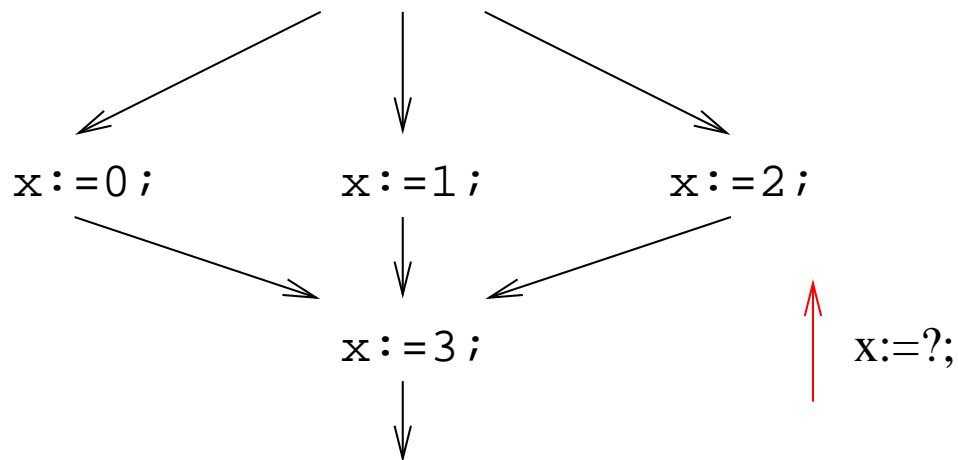
## ■ Redefinition



- $y:=x+1;$  is a reaching definition of  $y$ .

# Static Reverse Code Generation

- shown in [Akgul and Mooney, PASTE'02]
- Analyzes a source program
- Before executing a program
- Infeasible for non-deterministic programs



## Introduction

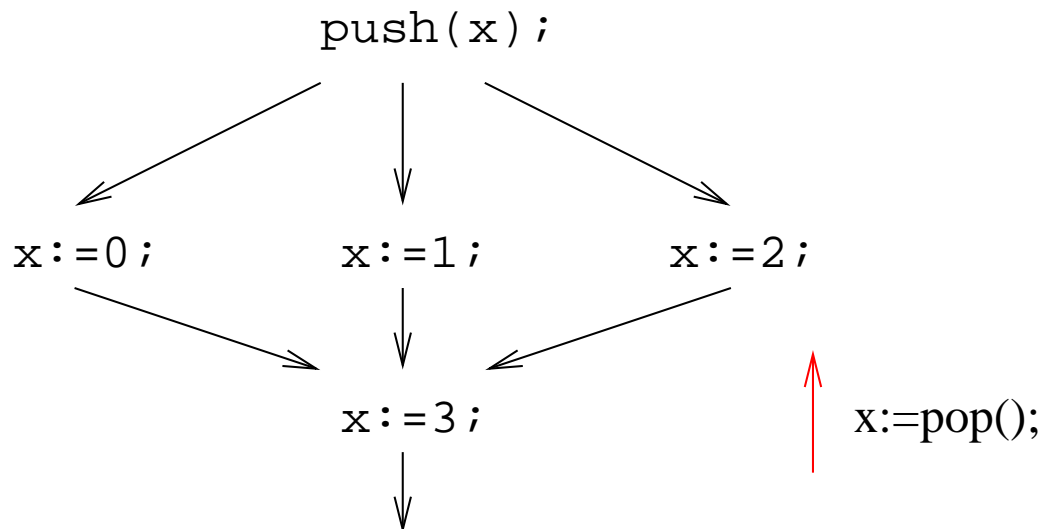
## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Static Reverse Code Generation

- shown in [Akgul and Mooney, PASTE'02]
- Analyzes a source program
- Before executing a program
- Infeasible for non-deterministic programs



## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Static Reverse Code Generation

- shown in [Akgul and Mooney, PASTE'02]
- Analyzes a source program
- Before executing a program
- Infeasible for non-deterministic programs
  
- Does it matter?



## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Static Reverse Code Generation

- shown in [Akgul and Mooney, PASTE'02]
- Analyzes a source program
- Before executing a program
- Infeasible for non-deterministic programs
  
- Does it matter?

**Yes, it does!**

Introduction

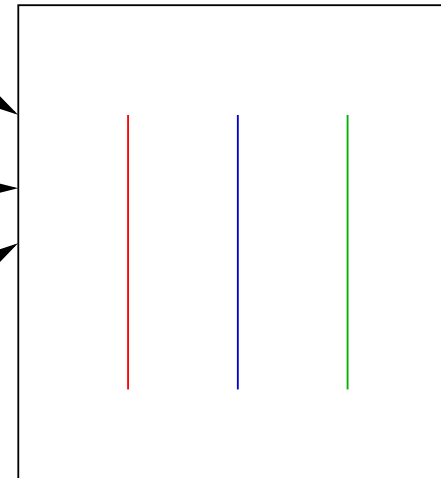
Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- **Static Reverse Code Generation**
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Multi-threaded Programs

- Multi-threaded programs occur everywhere.
- They are non-deterministic.



## Introduction

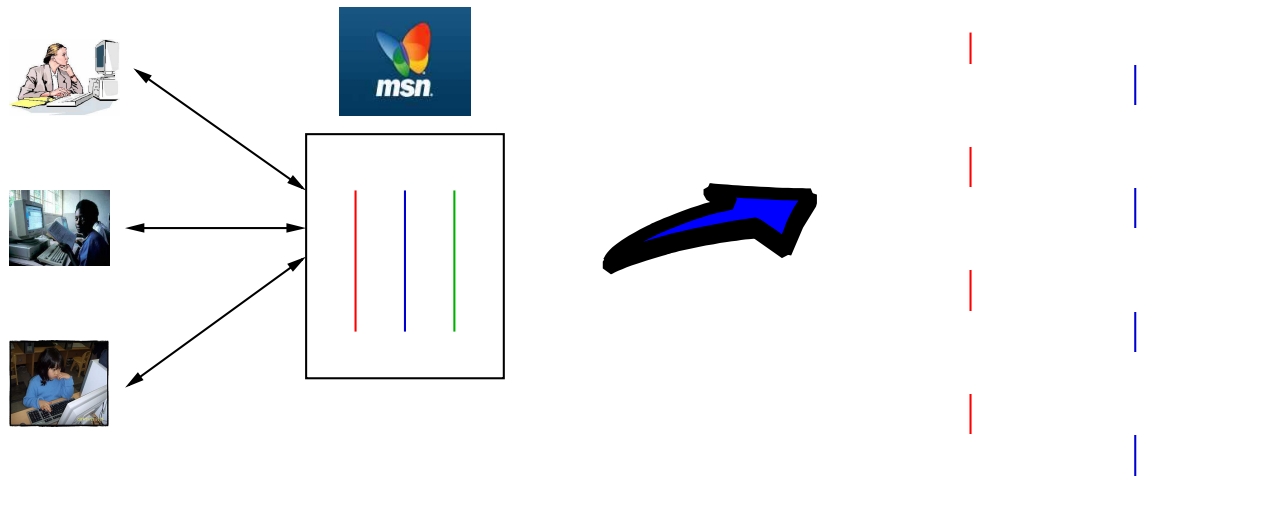
## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Multi-threaded Programs

- Multi-threaded programs occur everywhere.
- They are non-deterministic.
- Interleaving



## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation

## ● Multi-threaded Programs

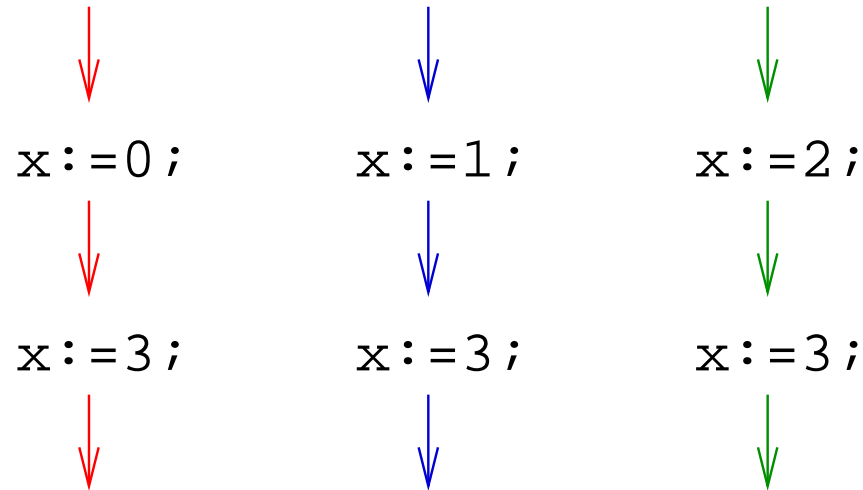
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



# Multi-threaded Programs

- Multi-threaded programs occur everywhere.
- They are non-deterministic.
- Interleaving



## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation

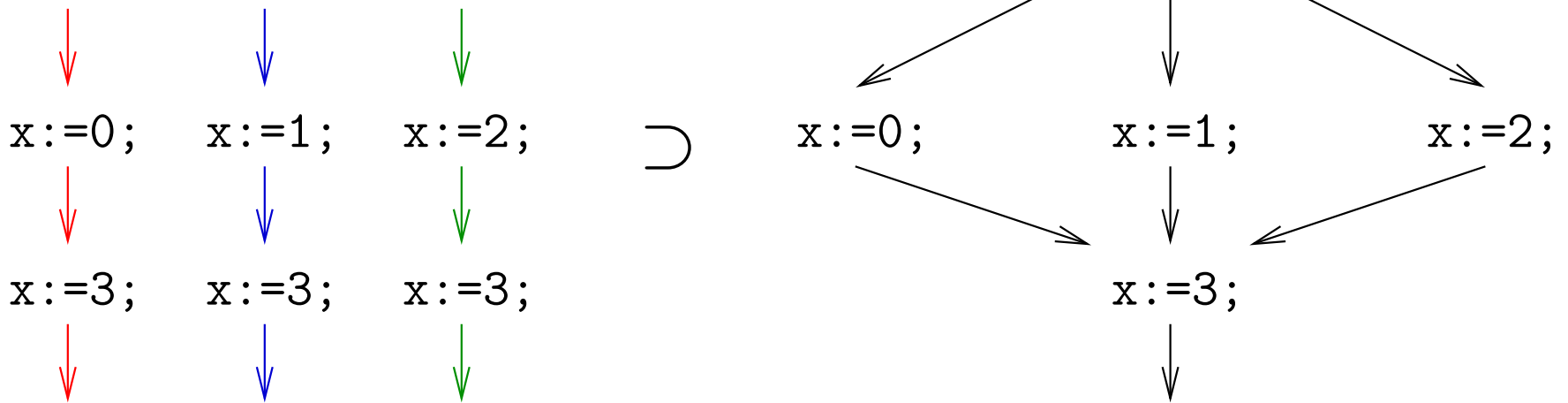
## ● Multi-threaded Programs

- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Multi-threaded Programs

- Multi-threaded programs occur everywhere.
- They are non-deterministic.
- Interleaving  $\Rightarrow$  Non-determinism



## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation

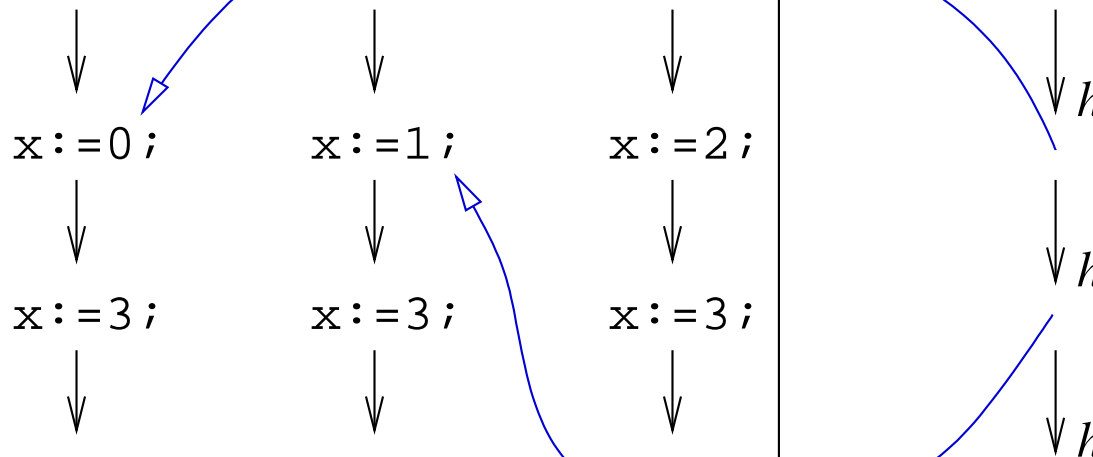
## Multi-threaded Programs

- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Dynamic Reverse Code Generation

- proposed in [Lee, V&D'06] and Chapter 5 of the dissertation
- Scales to multi-threaded programs
- Analyzes a runtime history of statements
- On-demand-basis generation at runtime
- A runtime history is essential for the reverse execution in non-deterministic programs, regardless of methods
- There is no way to infer non-deterministic choices



## Introduction

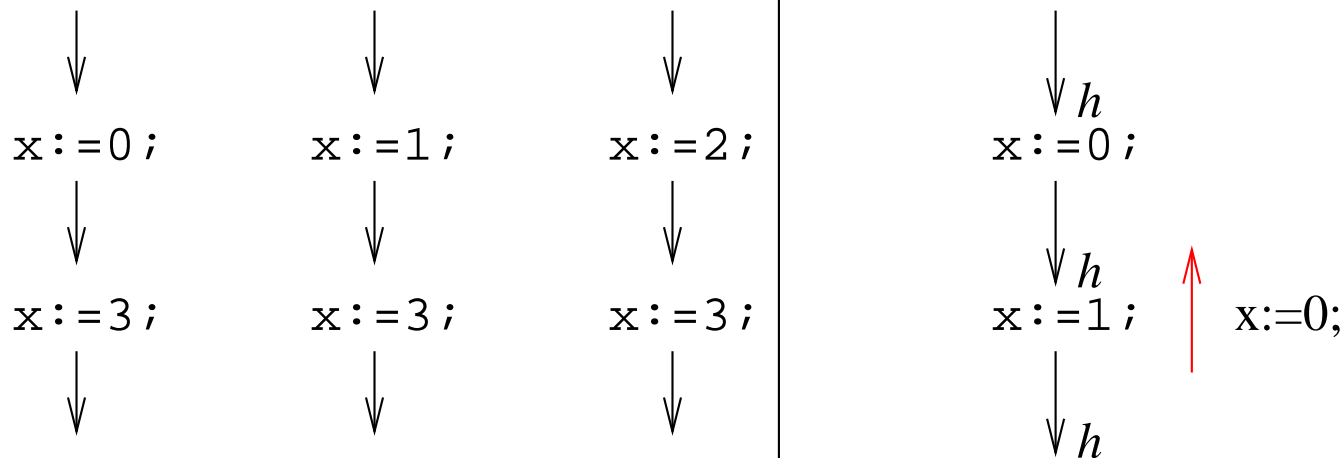
## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- **Dynamic Reverse Code Generation**
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Dynamic Reverse Code Generation

- proposed in [Lee, V&D'06] and Chapter 5 of the dissertation
- Scales to multi-threaded programs
- Analyzes a runtime history of statements
- On-demand-basis generation at runtime
- A runtime history is essential for the reverse execution in non-deterministic programs, regardless of methods
- There is no way to infer non-deterministic choices



## Introduction

### Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- **Dynamic Reverse Code Generation**
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

# Static vs. Dynamic Reverse Code Generation

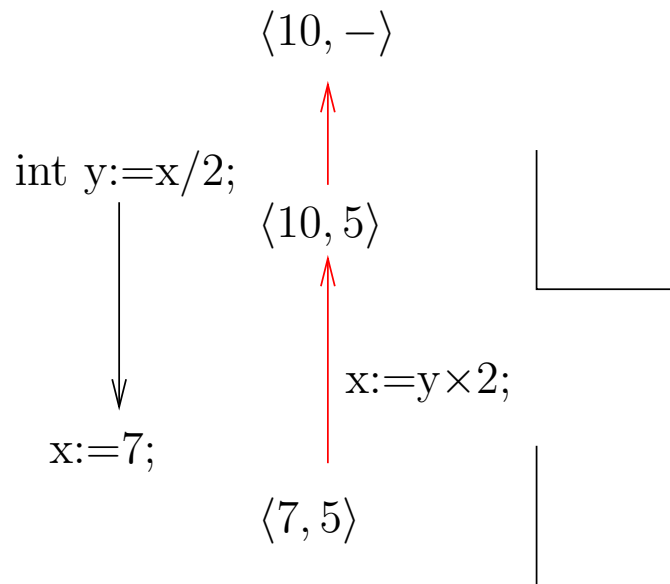
## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

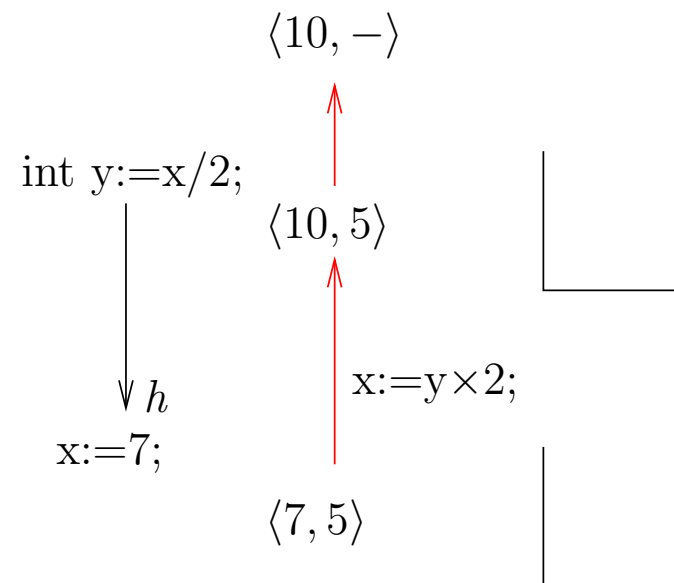
(Chapter 8)

- Source program
- Feasible only for deterministic programs
- Value-insensitive



- Minimal runtime overhead

- Runtime history
- Feasible for non-deterministic programs
- Value-sensitive



- Substantial runtime overhead
  - ◆ Multi-core processors
  - ◆ Interactive debugging

# Static vs. Dynamic Reverse Code Generation

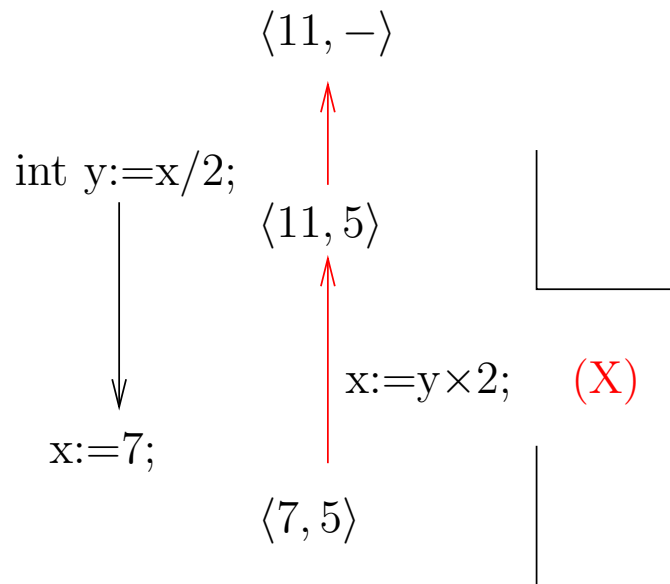
## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

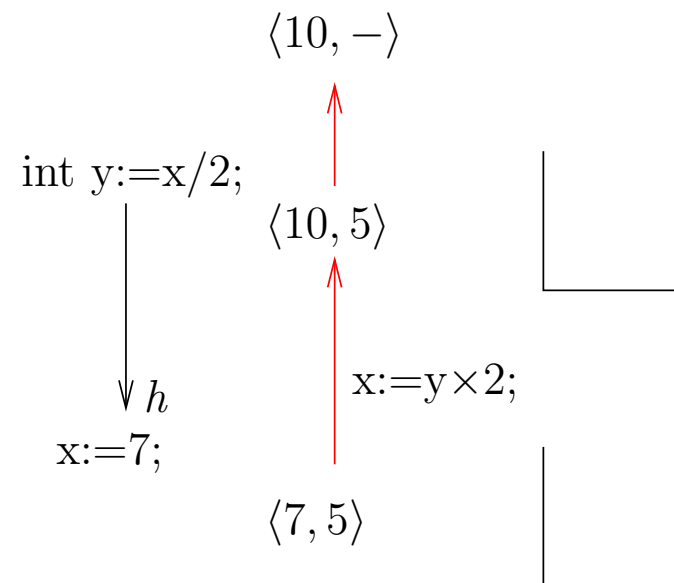
(Chapter 8)

- Source program
- Feasible only for deterministic programs
- Value-insensitive



- Minimal runtime overhead

- Runtime history
- Feasible for non-deterministic programs
- Value-sensitive



- Substantial runtime overhead
  - ◆ Multi-core processors
  - ◆ Interactive debugging

# Static vs. Dynamic Reverse Code Generation

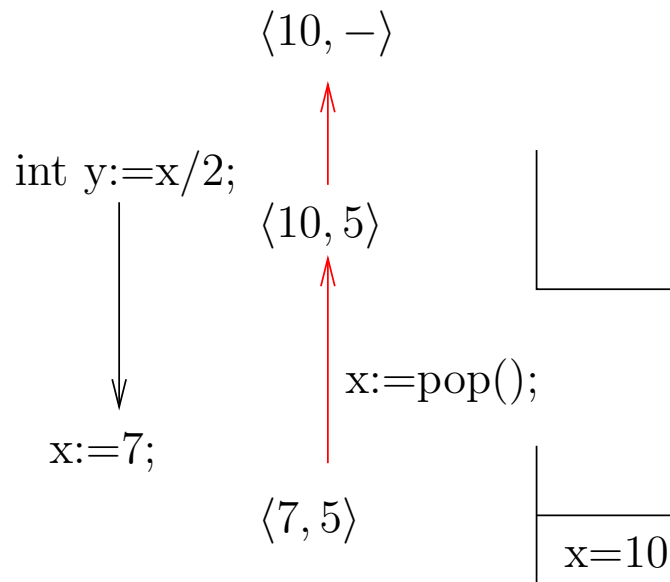
## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

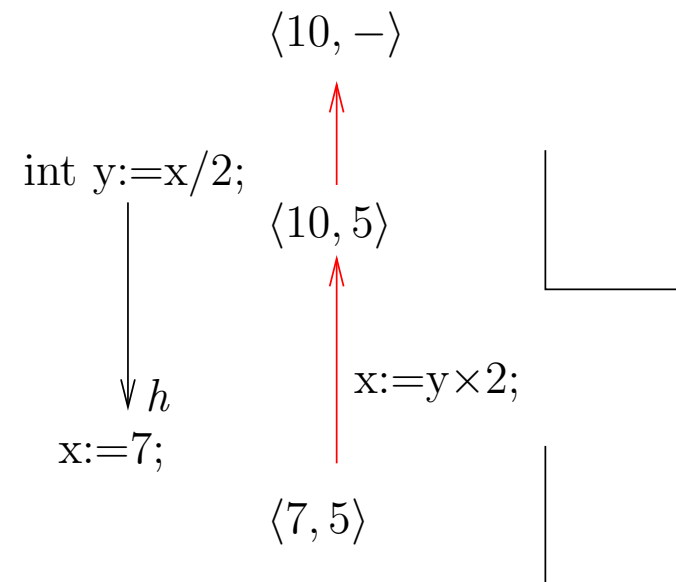
(Chapter 8)

- Source program
- Feasible only for deterministic programs
- Value-insensitive



- Minimal runtime overhead

- Runtime history
- Feasible for non-deterministic programs
- Value-sensitive



- Substantial runtime overhead
  - ◆ Multi-core processors
  - ◆ Interactive debugging

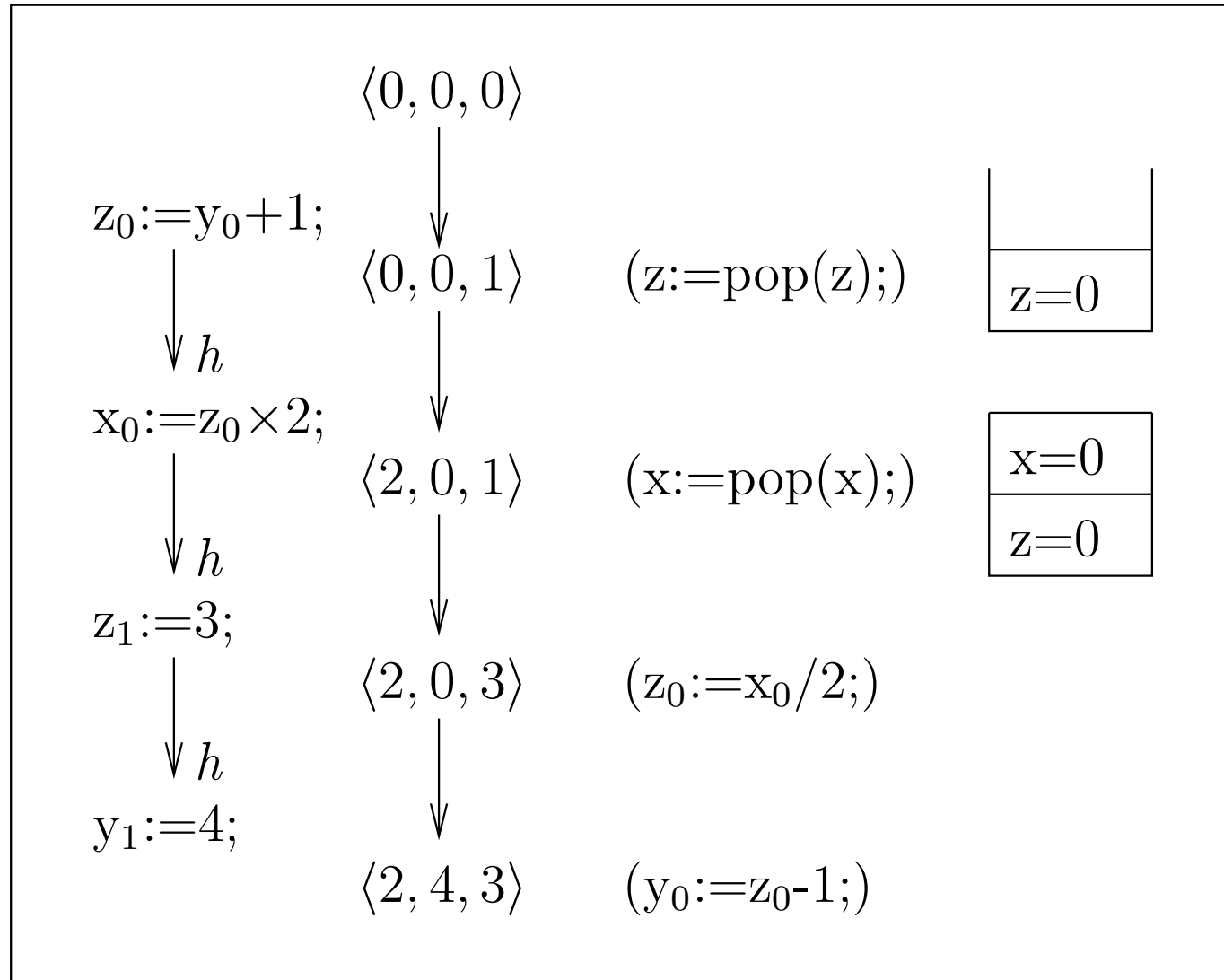
# Dynamic Reverse Code Generation

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)





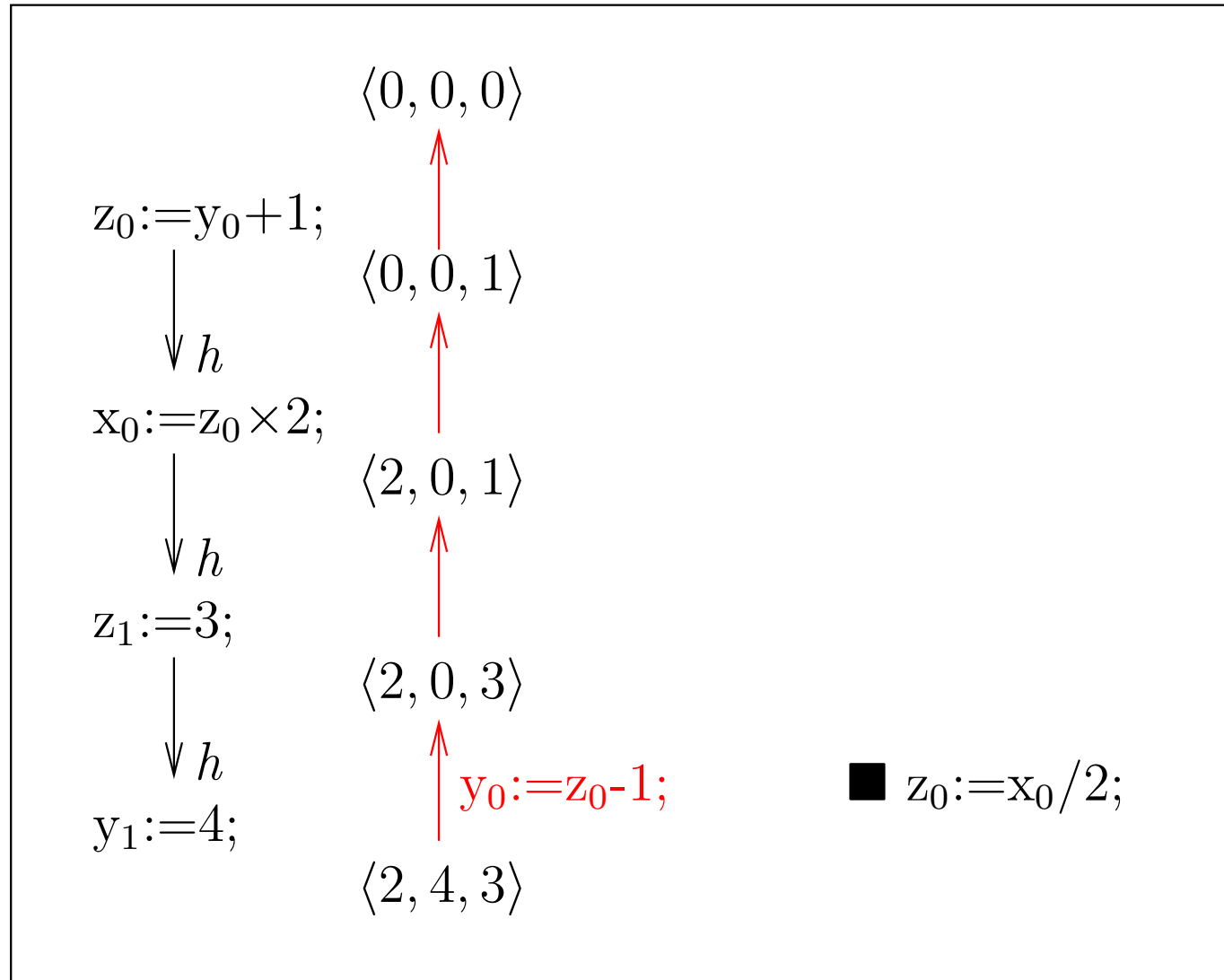
# Dynamic Reverse Code Generation

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



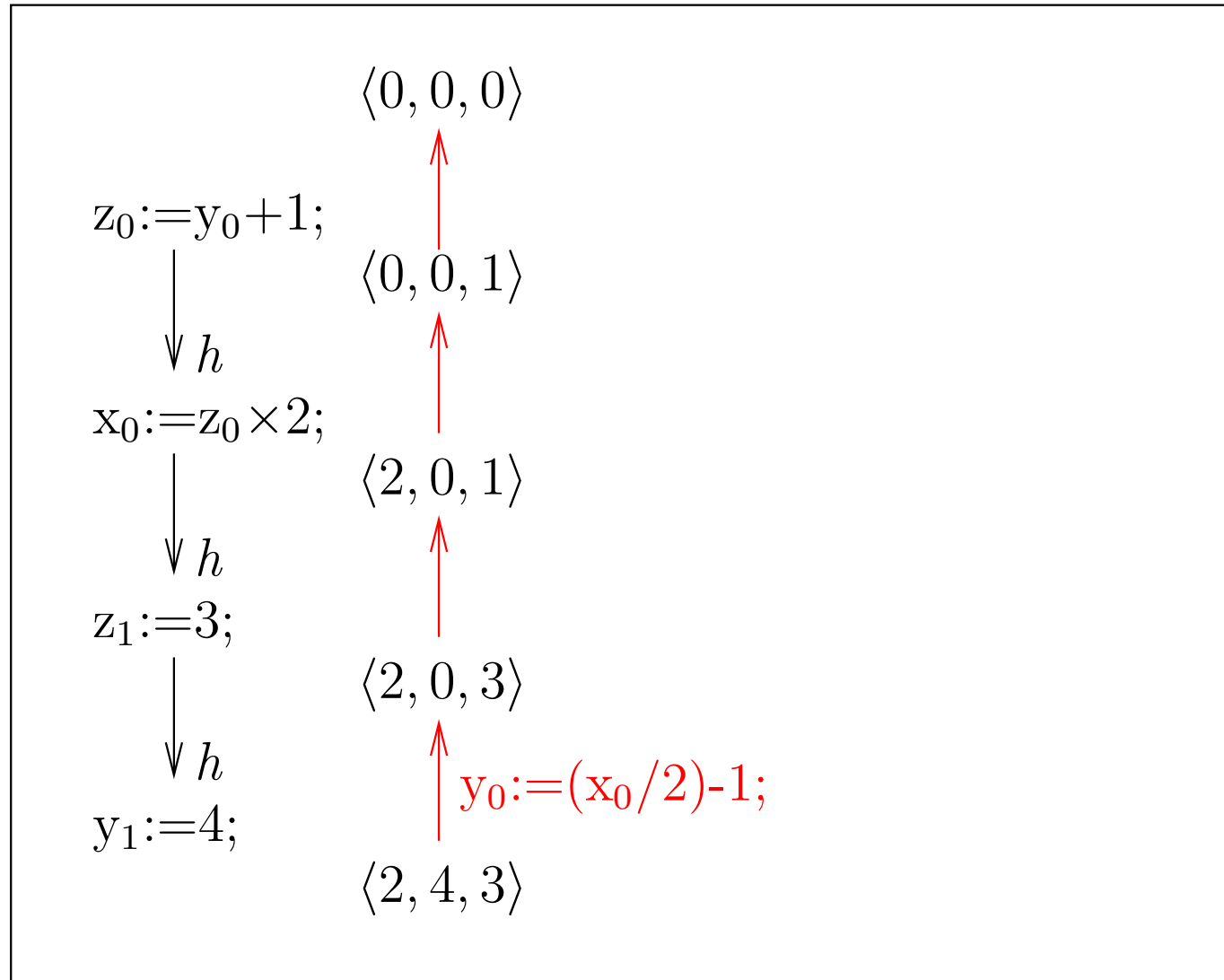
# Dynamic Reverse Code Generation

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



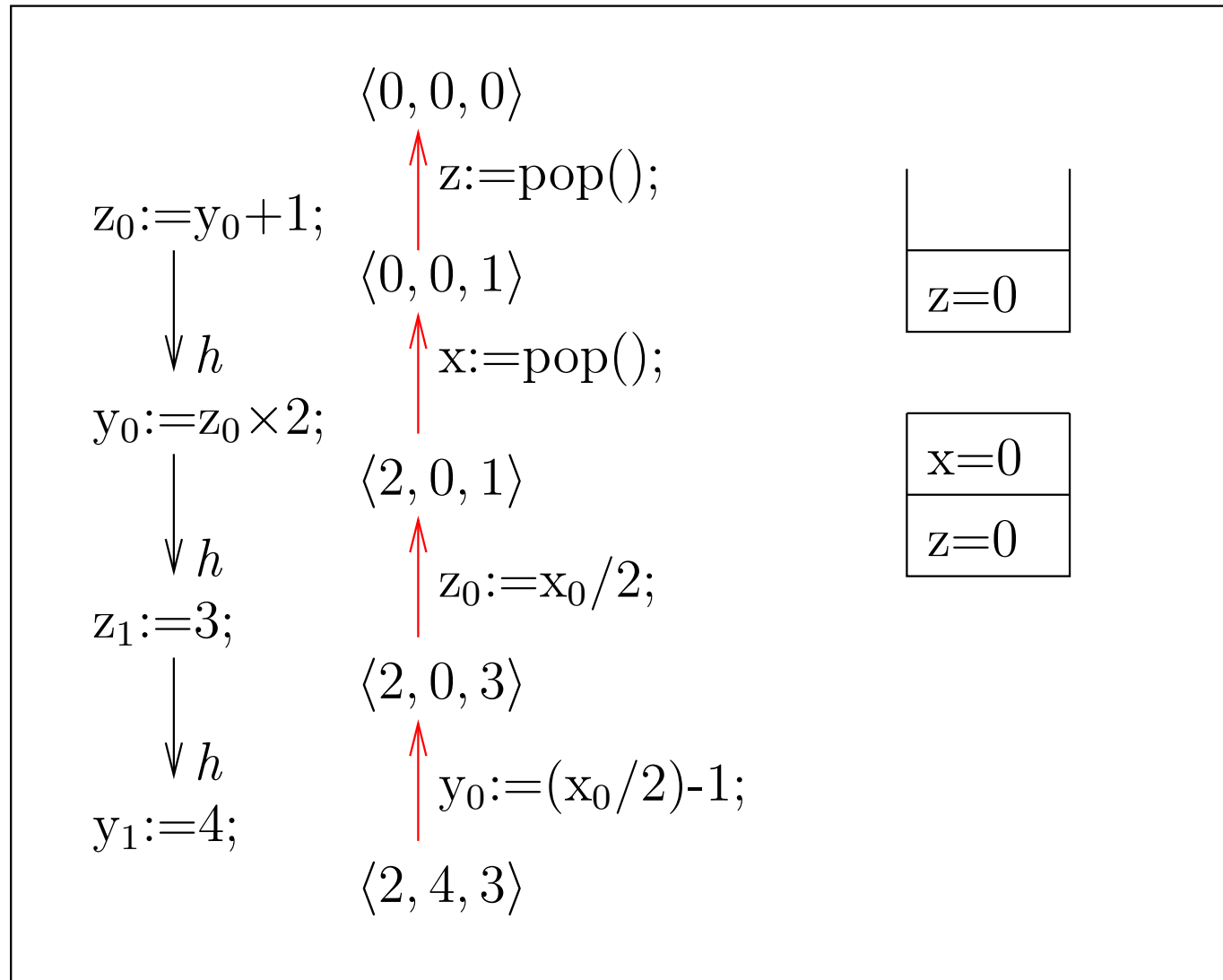
# Dynamic Reverse Code Generation

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



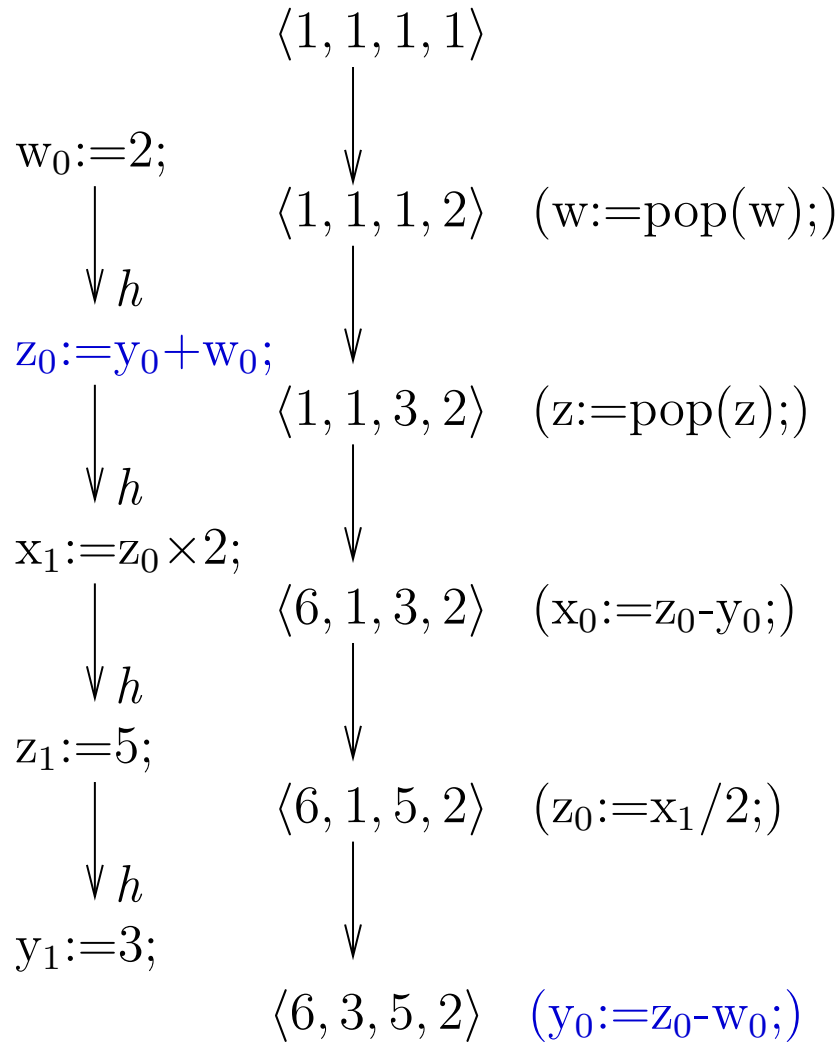
# Multiple Variables

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



$$\blacksquare z_0 = (\lambda t.t + w_0)(y_0)$$

$$\blacksquare (\lambda t.t + w_0)^{-1} = (\lambda t.t - w_0)$$

$$\blacksquare y_0 = (\lambda t.t - w_0)(z_0)$$

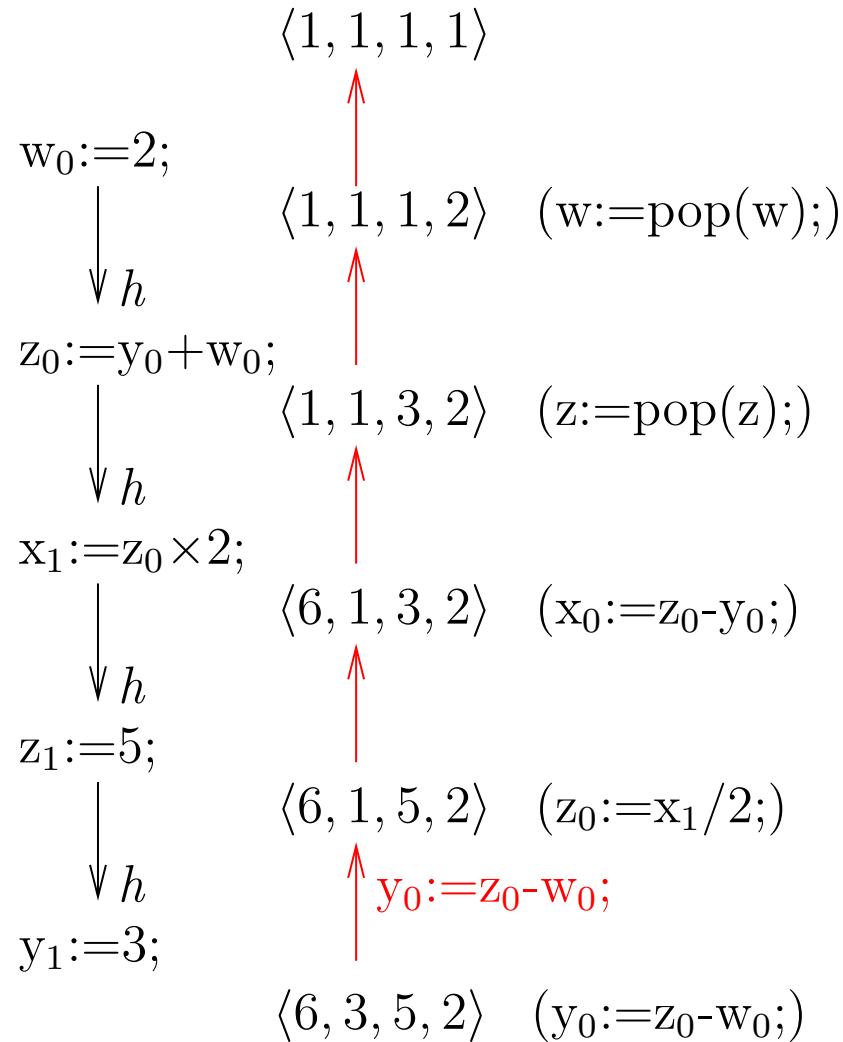
# Multiple Variables

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

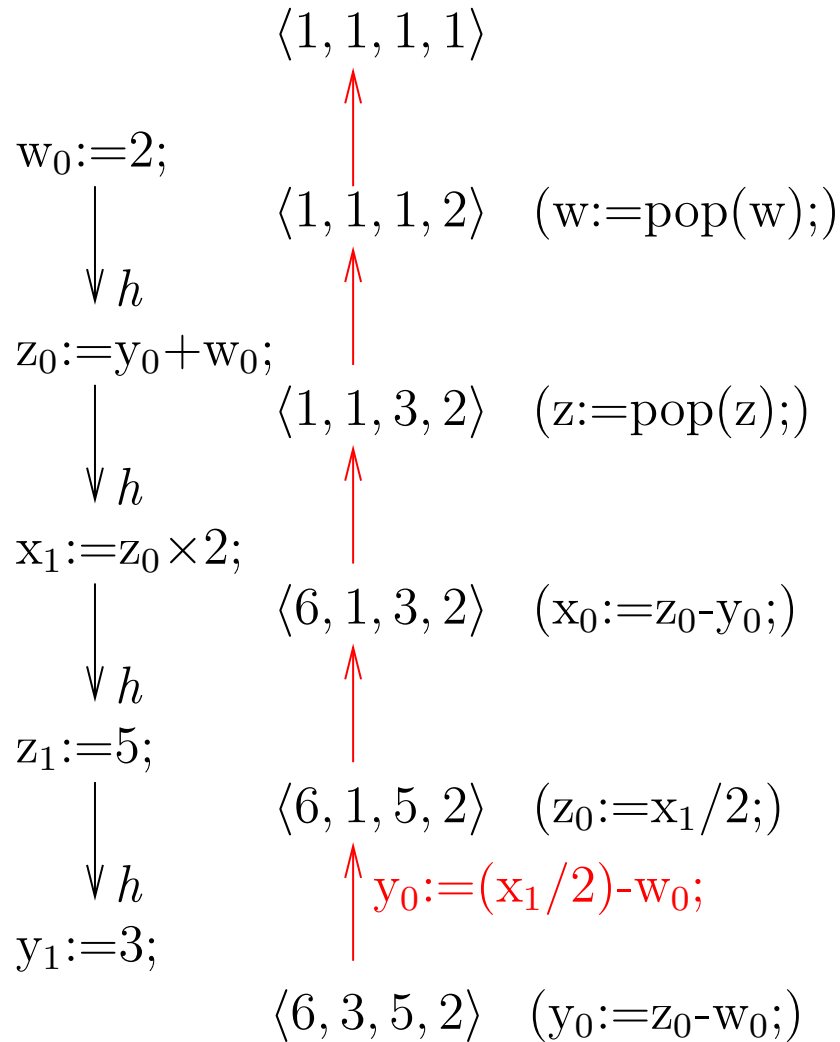


# Multiple Variables

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example



(Chapter 8)

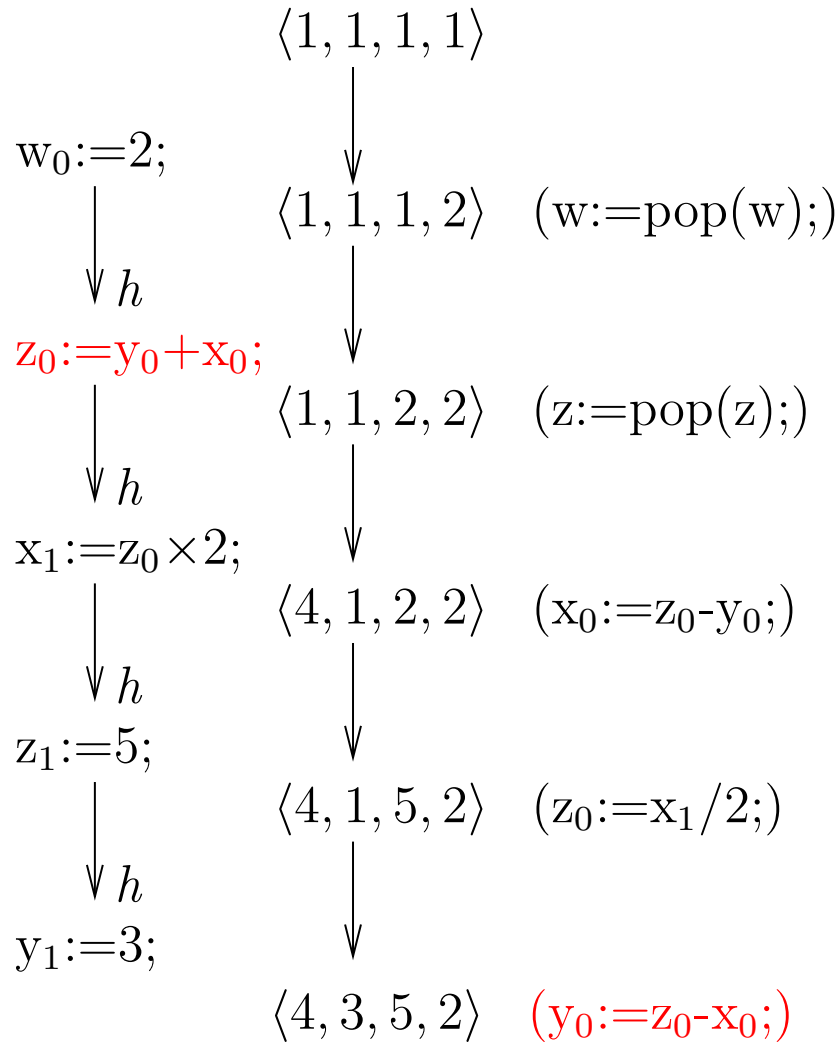
# Multiple Variables

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)



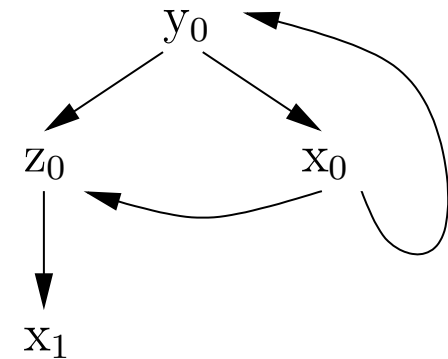
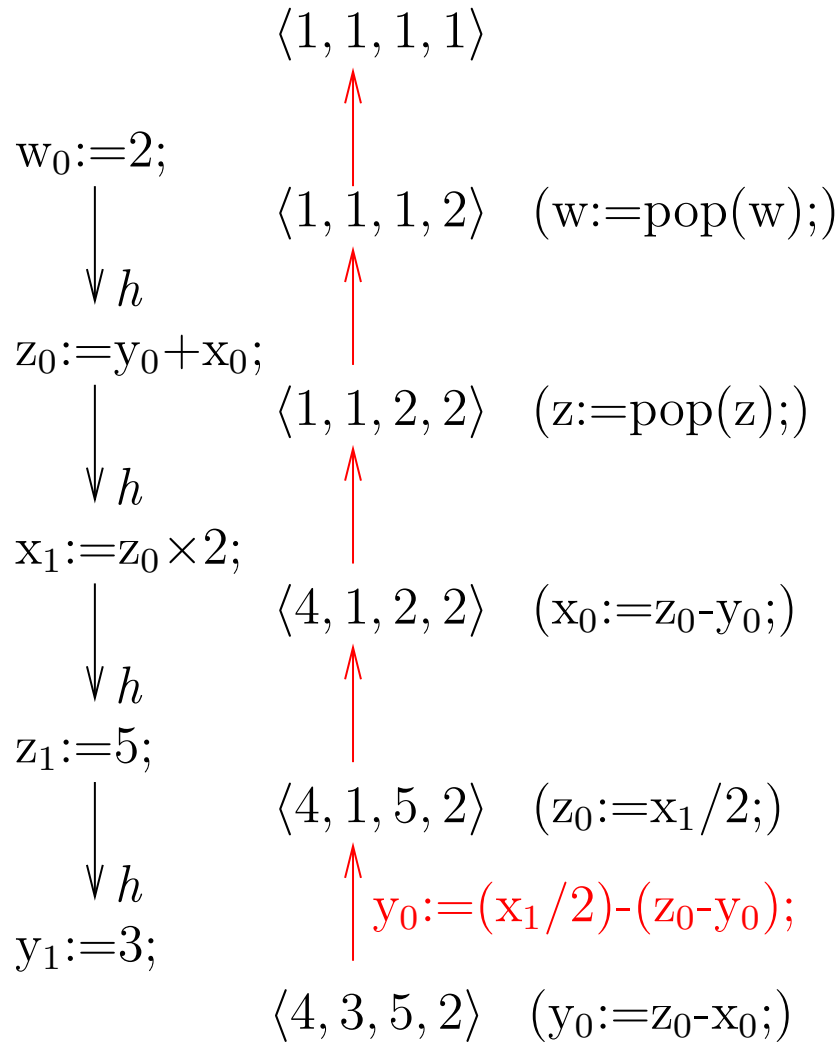
- $z_0 = (\lambda t.t + x_0)(y_0)$
- $(\lambda t.t + x_0)^{-1} = (\lambda t.t - x_0)$
- $y_0 = (\lambda t.t - x_0)(z_0)$

# Multiple Variables

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example



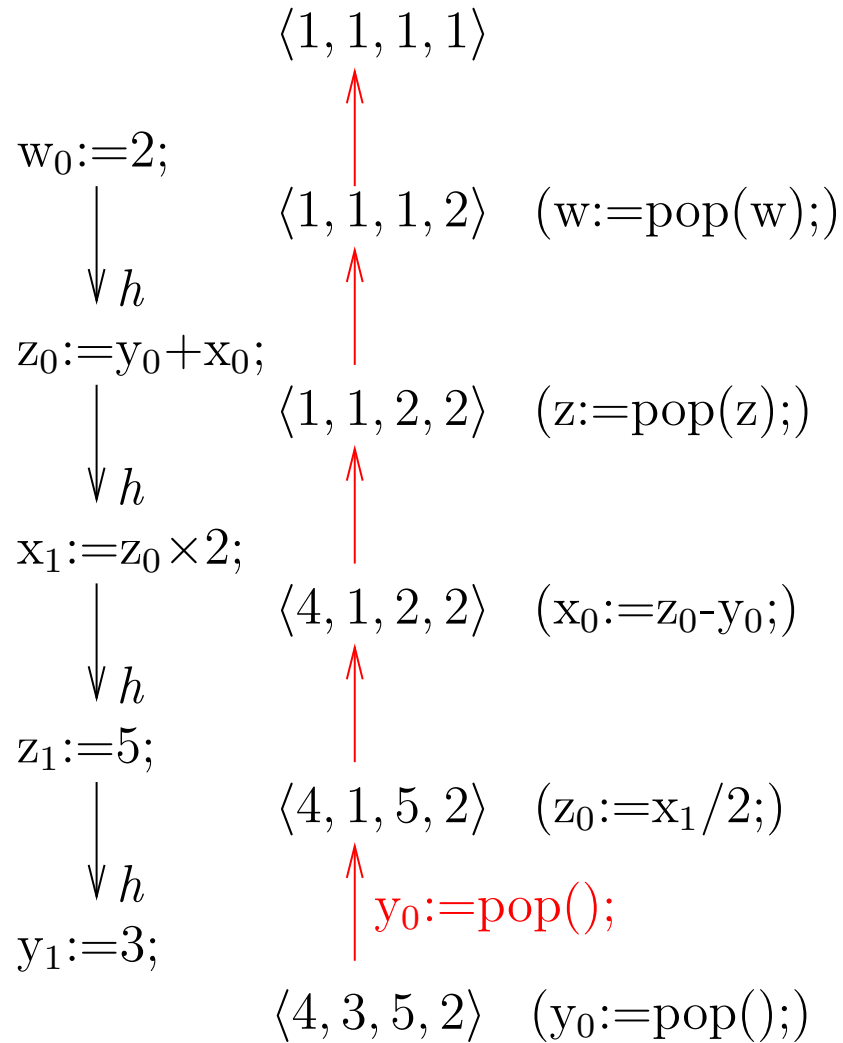


# Multiple Variables

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example



(Chapter 8)

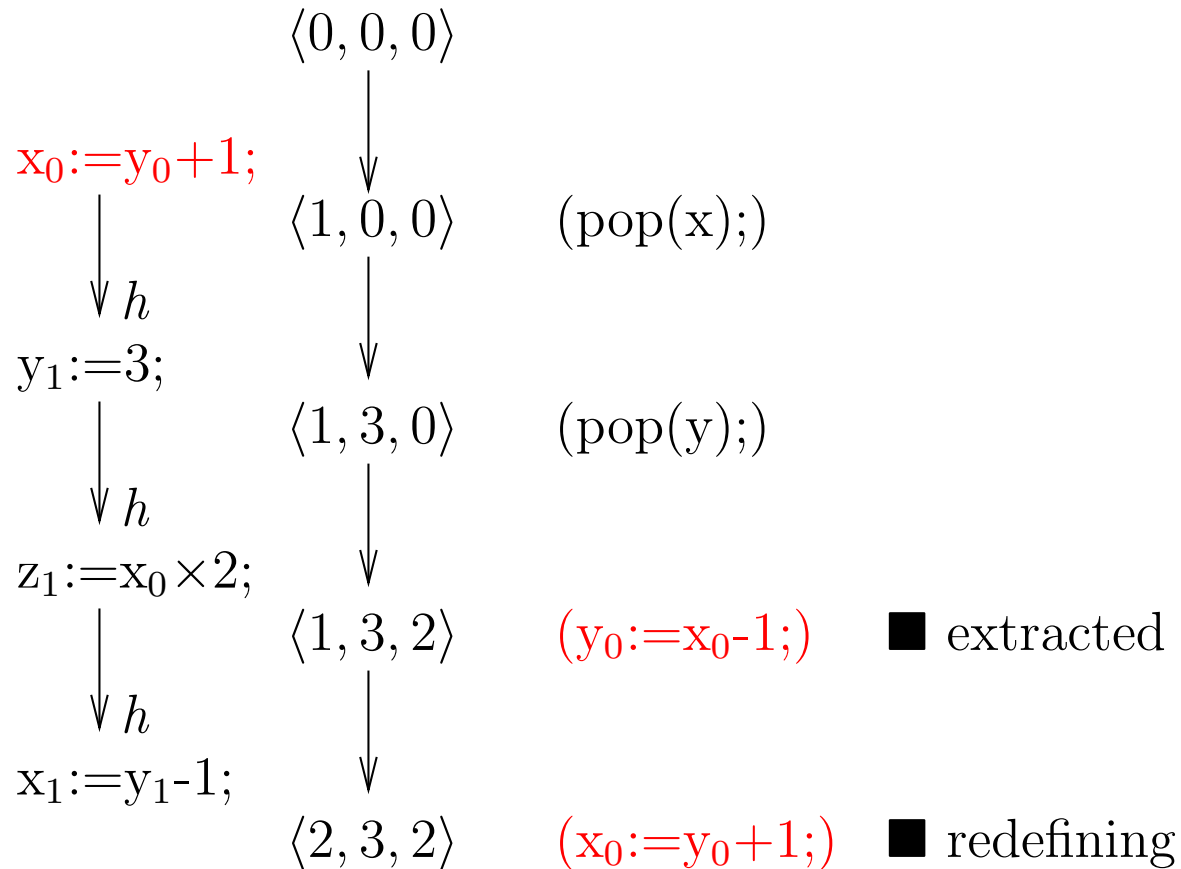
# Combination

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- **Combination**
- Soundness
- Bounded Buffer Example

(Chapter 8)

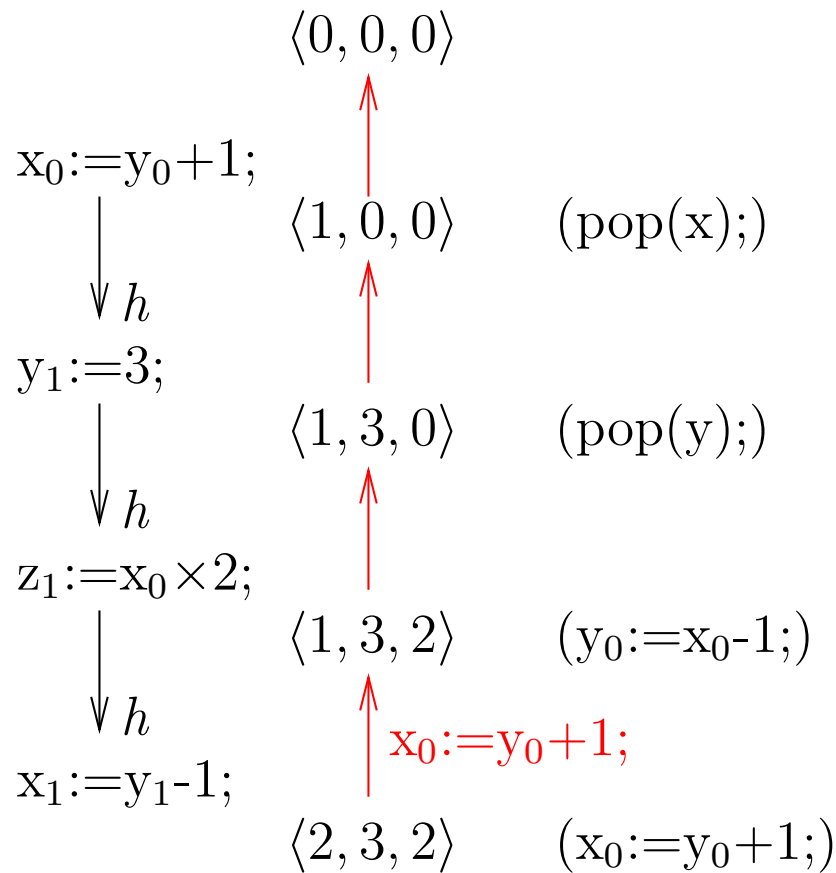


# Combination

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- **Combination**
- Soundness
- Bounded Buffer Example



(Chapter 8)

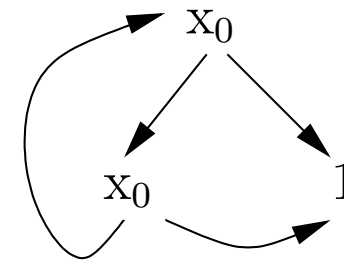
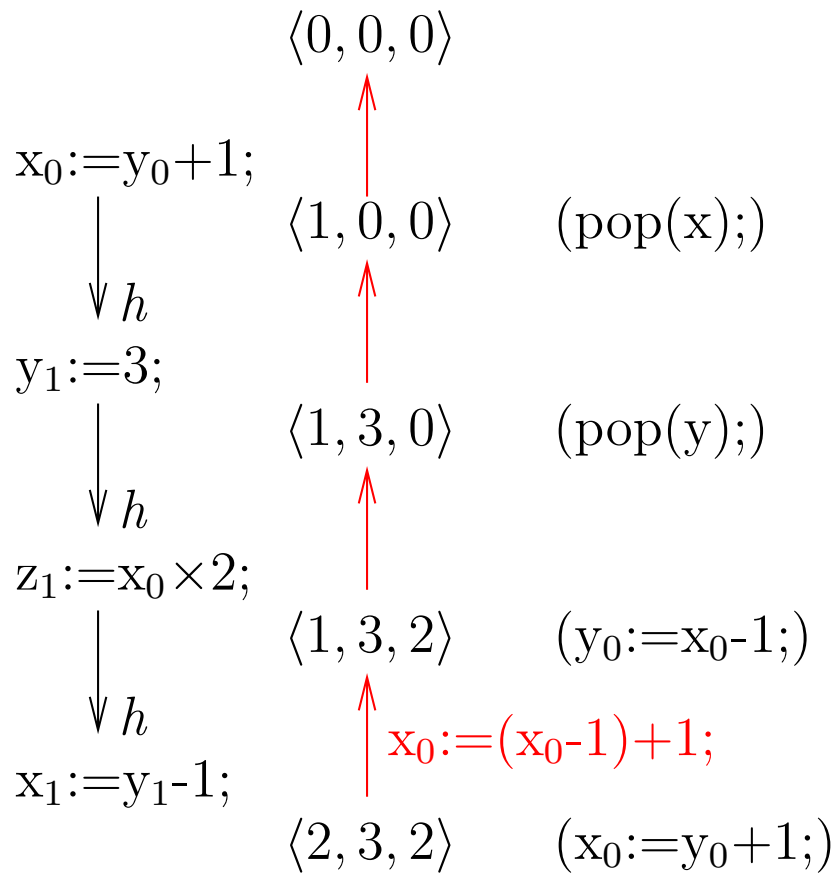
# Combination

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- **Combination**
- Soundness
- Bounded Buffer Example

(Chapter 8)



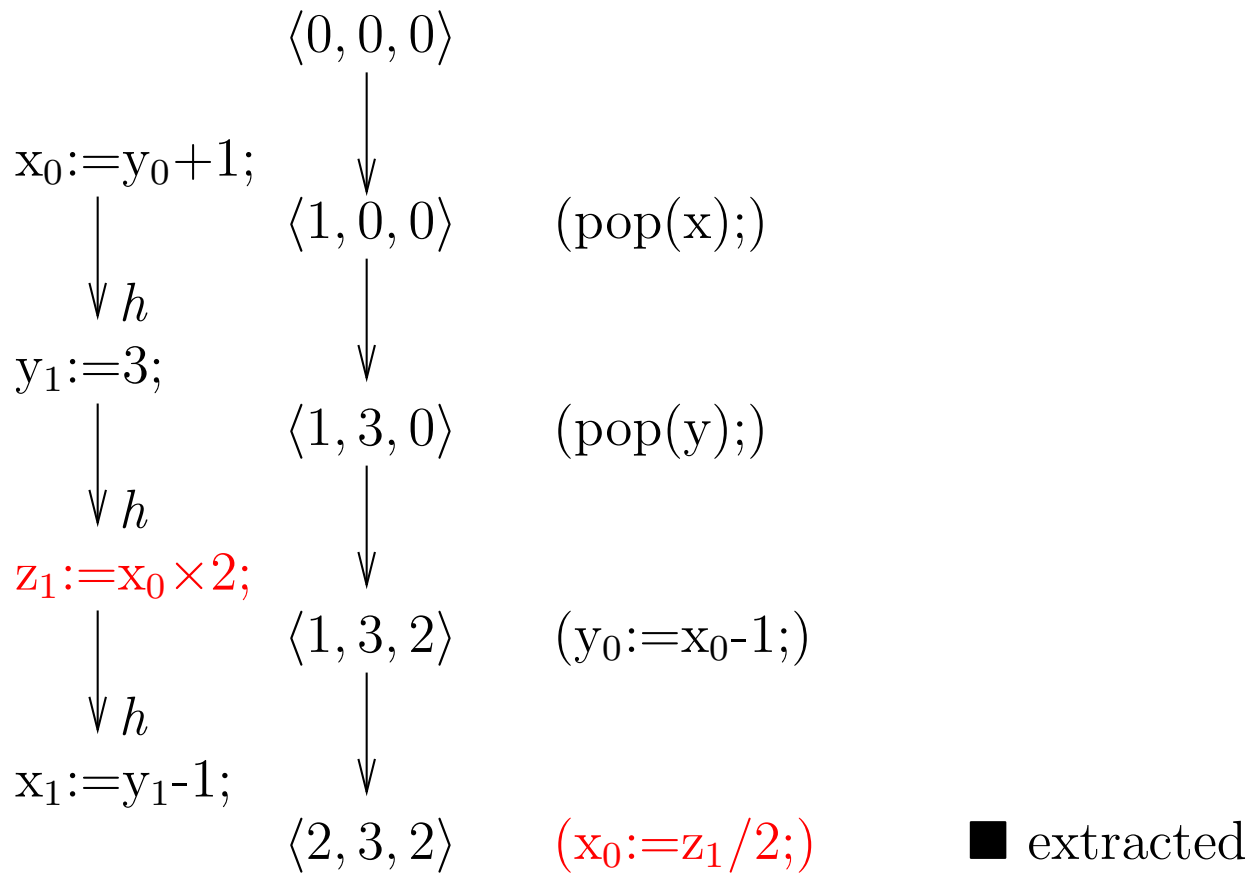
# Combination

## Introduction

## Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- **Combination**
- Soundness
- Bounded Buffer Example

(Chapter 8)



# Soundness

The value of  $v$  restored by dynamic reverse code generation is the same as the previous value of  $v$ .

*Proof.* Suppose that the reverse code for  $v$  is  $v := f(u_1, u_2, \dots, u_n)$

1. The value of  $u_k$  either is immediately available or can be restored.
2. A reverse code is deterministically calculated.
3. The restoration of  $u_k$  does not involve  $v$ .

□

- A deterministic algorithm exploiting extraction-from-use was shown in [Lee, V&D'06].
- Conjecture: also true when redefinition/combination is used.

Introduction

Reverse Execution

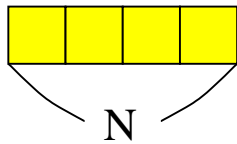
- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example

(Chapter 8)

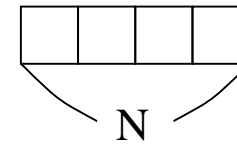
# Bounded Buffer Example (Chapter 8)

- It is widely used.

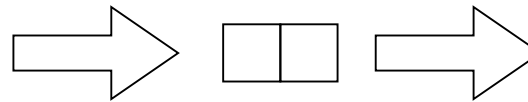
Producer



Consumer



bounded buffer



Introduction

Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example (Chapter 8)

# Bounded Buffer Example (Chapter 8)

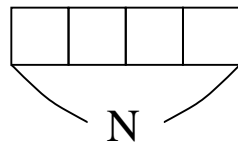
Introduction

Reverse Execution

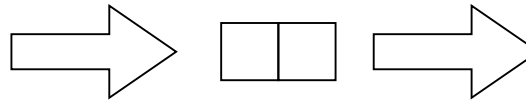
- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example (Chapter 8)

- It is widely used.

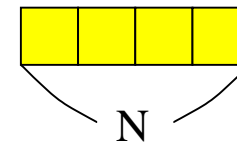
Producer



bounded buffer



Consumer





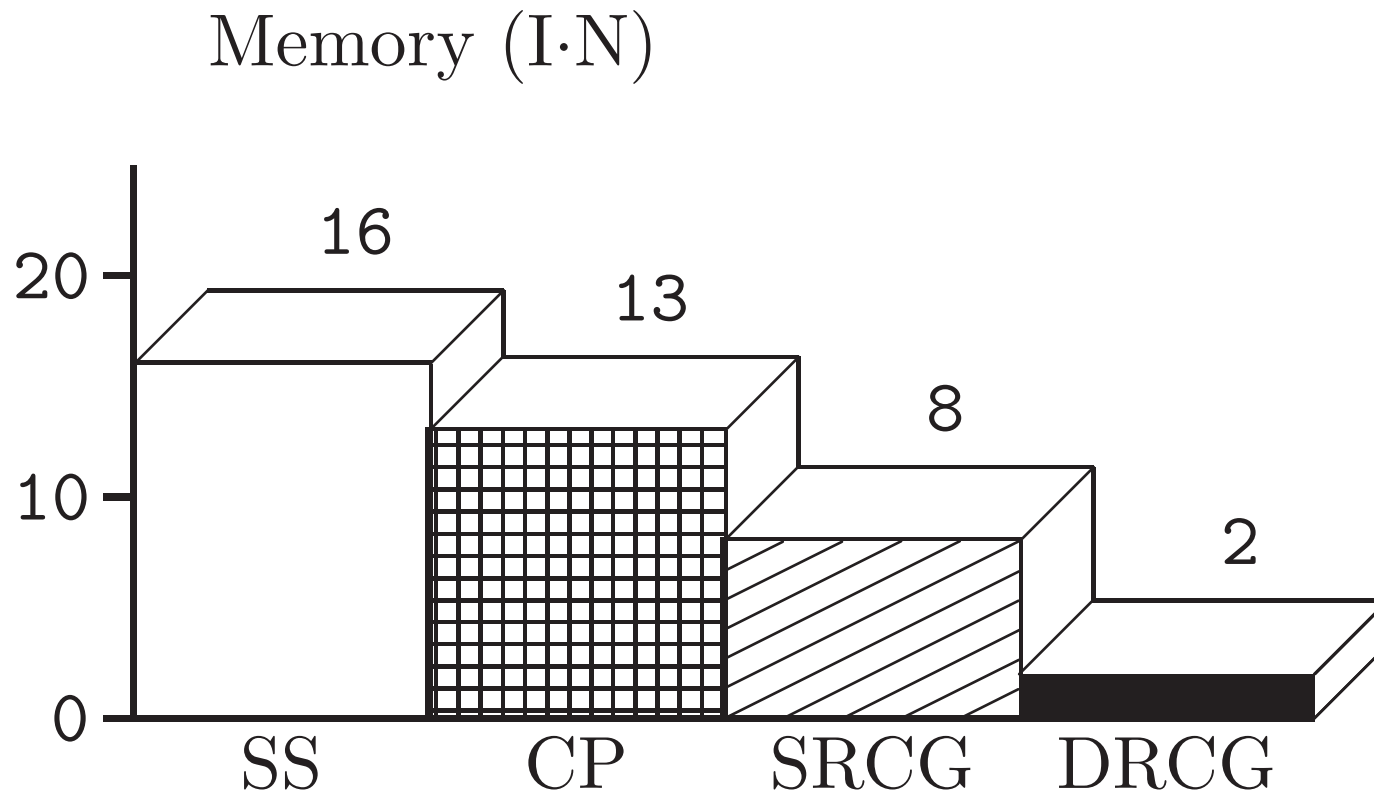
# Bounded Buffer Example (Chapter 8)

Introduction

Reverse Execution

- What?
- Locating a Bug
- Locating a Bug by Iterative Execution
- Locating a Bug by Reverse Execution
- Reverse-Execution Methods
- Loop Example
- Reverse Execution by State-Saving
- Reverse Execution by Checkpointing
- Reverse Execution by Checkpointing
- Reverse Execution by Reverse Code
- Reverse Code Generation
- Static Reverse Code Generation
- Multi-threaded Programs
- Dynamic Reverse Code Generation
- Static vs. Dynamic Reverse Code Generation
- Dynamic Reverse Code Generation
- Multiple Variables
- Combination
- Soundness
- Bounded Buffer Example (Chapter 8)

- It is widely used.



Introduction

Reverse Execution

**Program Validation by  
Symbolic Execution**

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL  
Tree

Concluding Remarks

# Program Validation by Symbolic Execution

# Testing

Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

● Testing

● Symbolic Execution

● Heap

● Symbolic Execution on Heap

● Constraint Solver

● Lazy Initialization

● Lazier Initialization

● Lazy vs. Lazier

● Loop Example

● Solutions

● Bounded Symbolic Execution

● Soundness

● Completeness

● Insertion Procedure of AVL  
Tree

Concluding Remarks

..., {x=-1}, {x=0}, {x=1}, ...



..., {posinc(-1)=-1}, {posinc(0)=0}, {posinc(1)=2}, ...

■ How many input/output pairs?

# Symbolic Execution

Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

● Testing

● Symbolic Execution

● Heap

● Symbolic Execution on Heap

● Constraint Solver

● Lazy Initialization

● Lazier Initialization

● Lazy vs. Lazier

● Loop Example

● Solutions

● Bounded Symbolic Execution

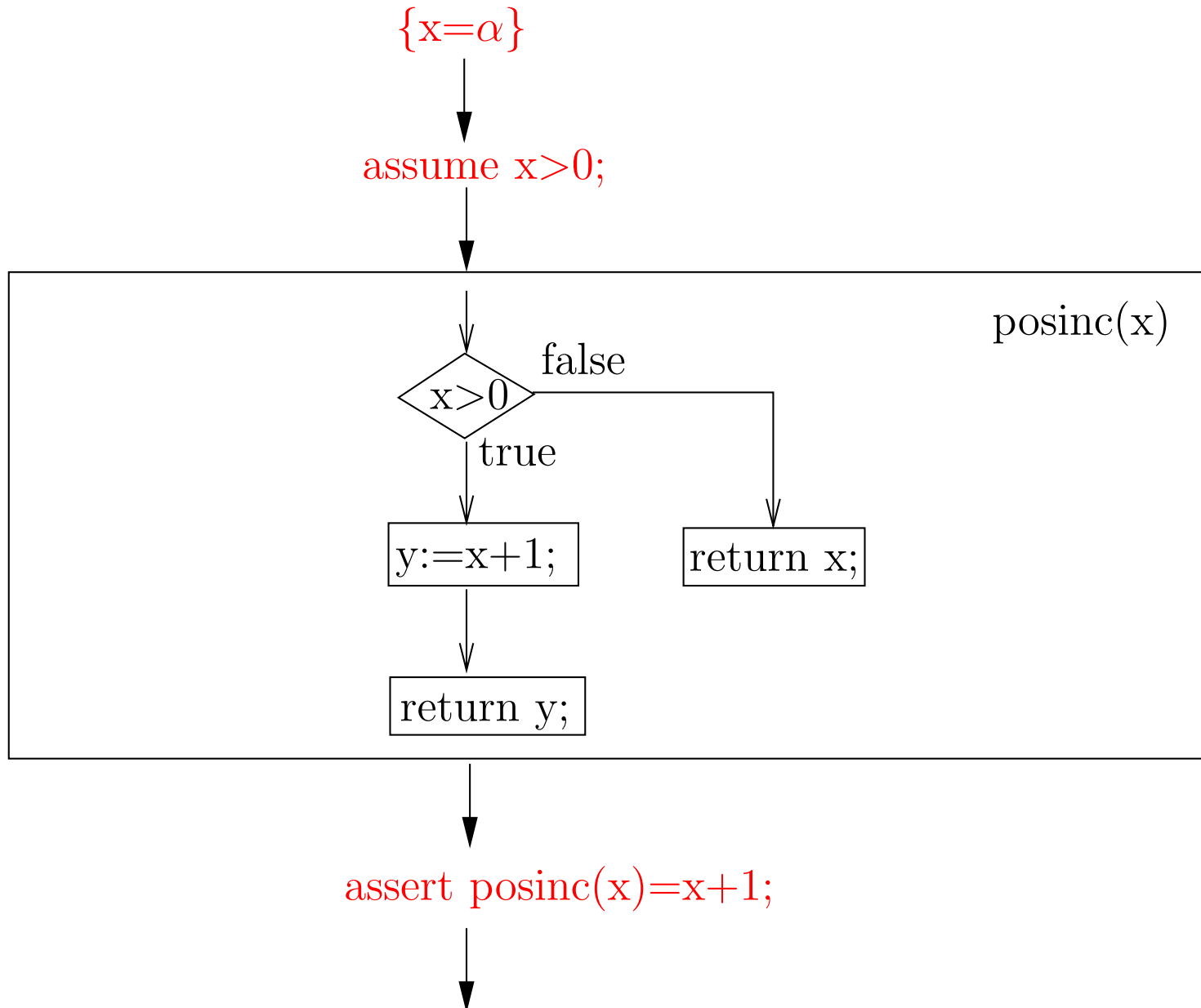
● Soundness

● Completeness

● Insertion Procedure of AVL

Tree

Concluding Remarks



# Symbolic Execution

Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

● Testing

● Symbolic Execution

● Heap

● Symbolic Execution on Heap

● Constraint Solver

● Lazy Initialization

● Lazier Initialization

● Lazy vs. Lazier

● Loop Example

● Solutions

● Bounded Symbolic Execution

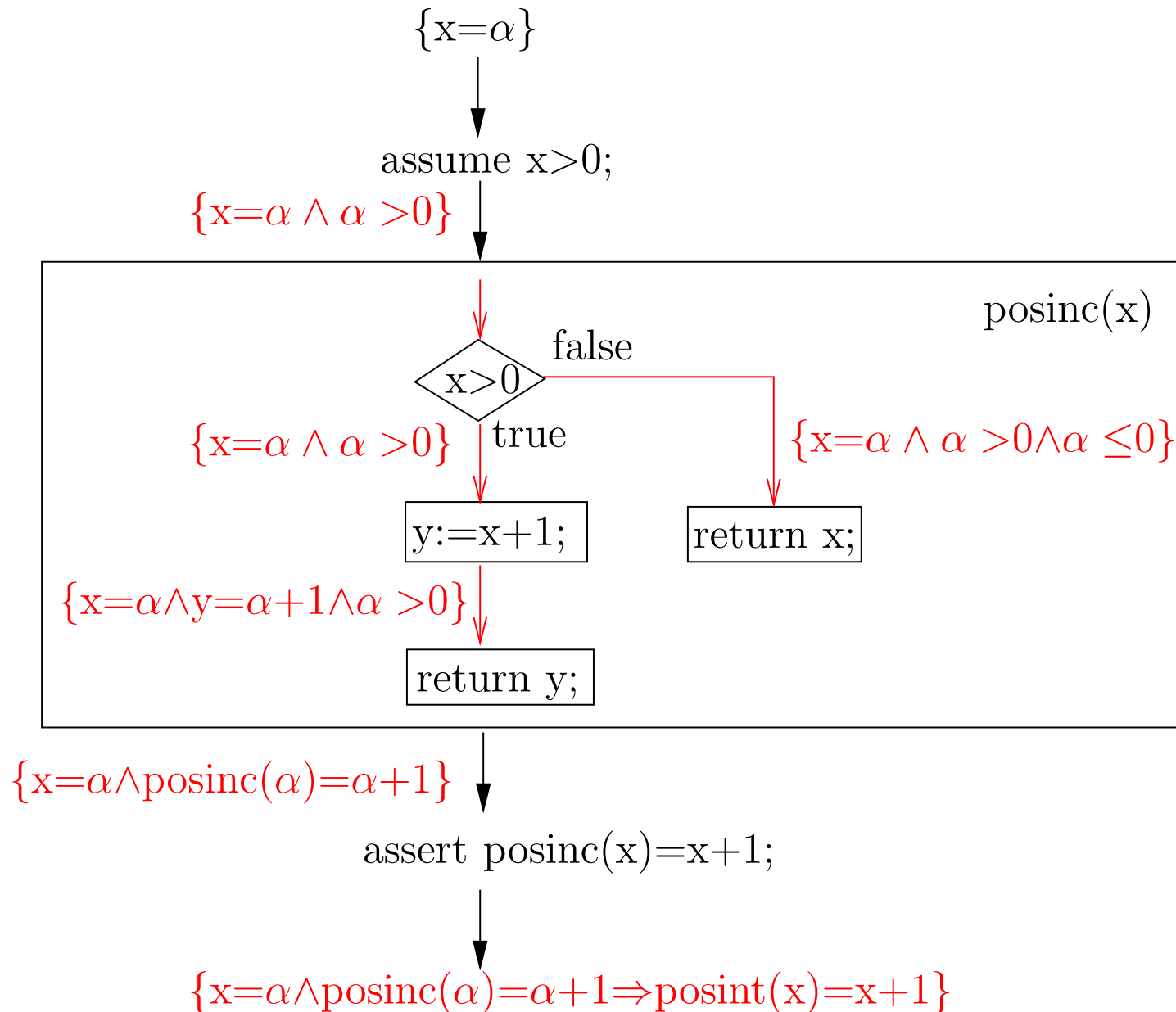
● Soundness

● Completeness

● Insertion Procedure of AVL

Tree

Concluding Remarks



# Heap

Introduction

Reverse Execution

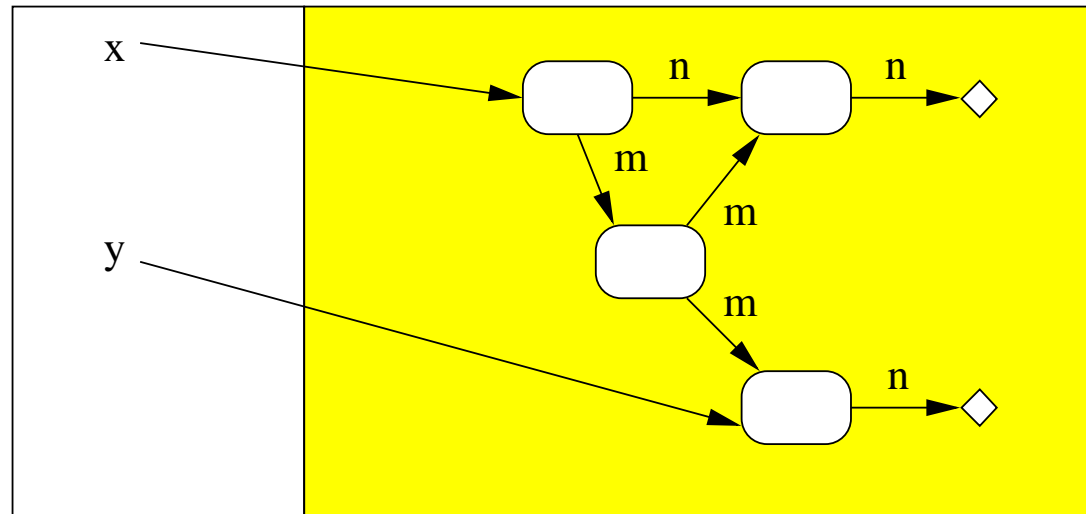
Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution

● **Heap**

- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL  
Tree

Concluding Remarks



# Symbolic Execution on Heap

Introduction

---

Reverse Execution

---

Program Validation by  
Symbolic Execution

---

- Testing
- Symbolic Execution
- Heap
- **Symbolic Execution on Heap**
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL  
Tree

Concluding Remarks

---

$$\{x = \alpha \wedge \alpha \mapsto [f : \beta]\}$$

$y := x.f;$

$$\{x = \alpha \wedge y = \beta \wedge \alpha \mapsto [f : \beta]\}$$

$$\{x = \alpha \wedge y = \beta \wedge \beta \mapsto [f : -]\}$$

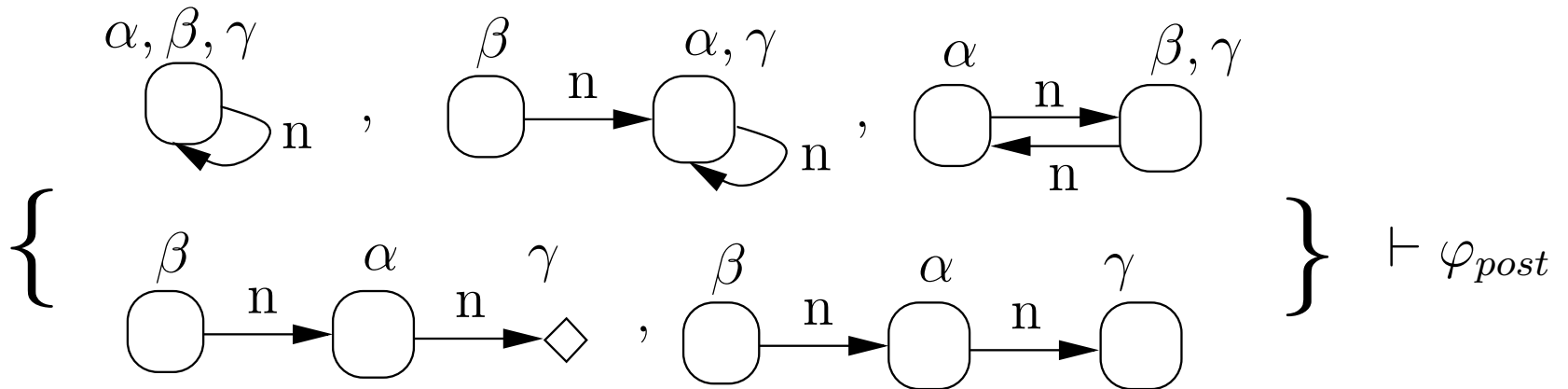
$y.f := x;$

$$\{x = \alpha \wedge y = \beta \wedge \beta \mapsto [f : \alpha]\}$$

# Constraint Solver

$$\{c = \alpha \wedge t = \beta \wedge s = \gamma \wedge \alpha \mapsto [n : \gamma] \wedge \beta \mapsto [n : \alpha]\}$$

assert  $\varphi_{post}$ ;

$$\{c = \alpha \wedge t = \beta \wedge s = \gamma \wedge \alpha \mapsto [n : \gamma] \wedge \beta \mapsto [n : \alpha] \Rightarrow \varphi_{post}\}$$


$$\vdash \varphi_{post}$$

Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap

● **Constraint Solver**

- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks



# Lazy Initialization

Introduction

Reverse Execution

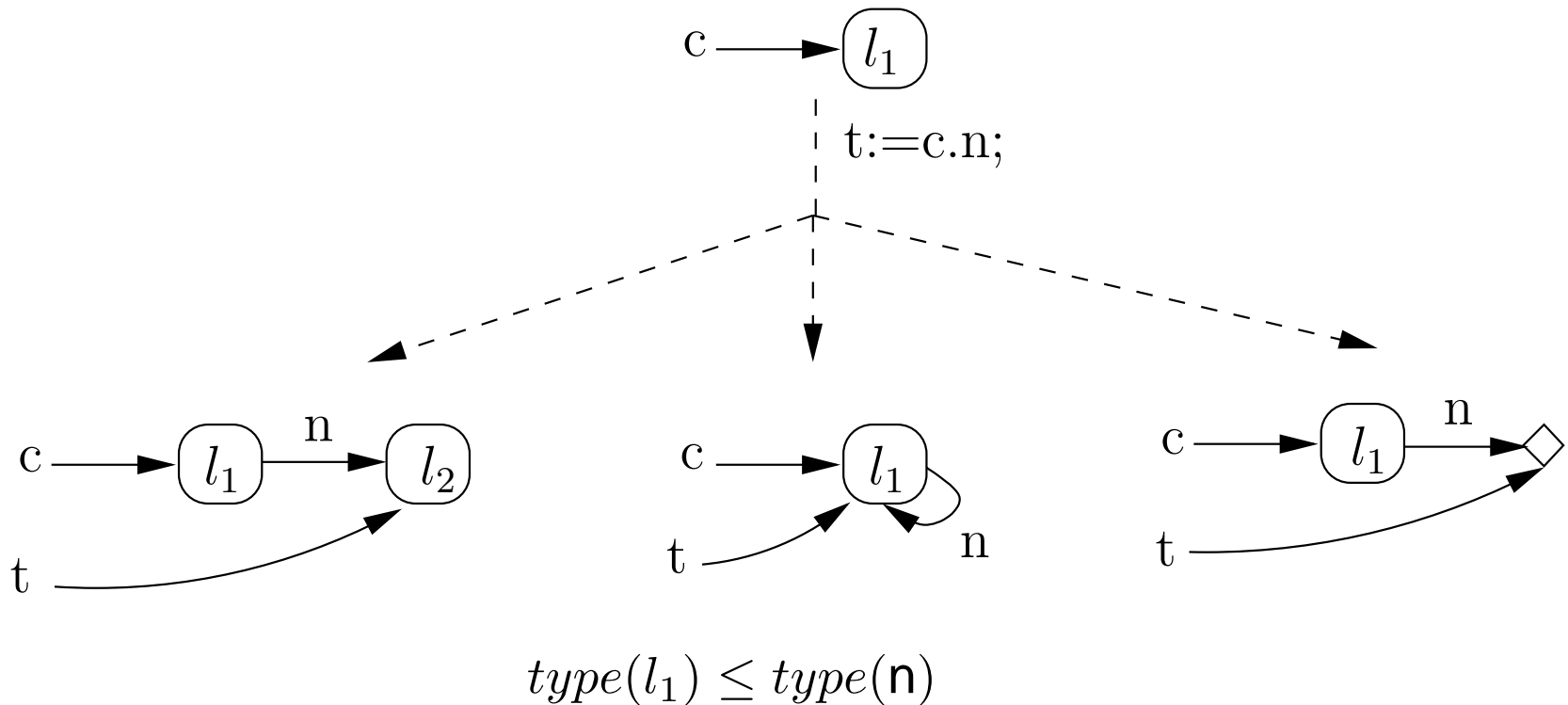
Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- **Lazy Initialization**

- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks

- introduced in [Khurshid, Păsăreanu and Visser, TACAS'03]



# Lazy Initialization

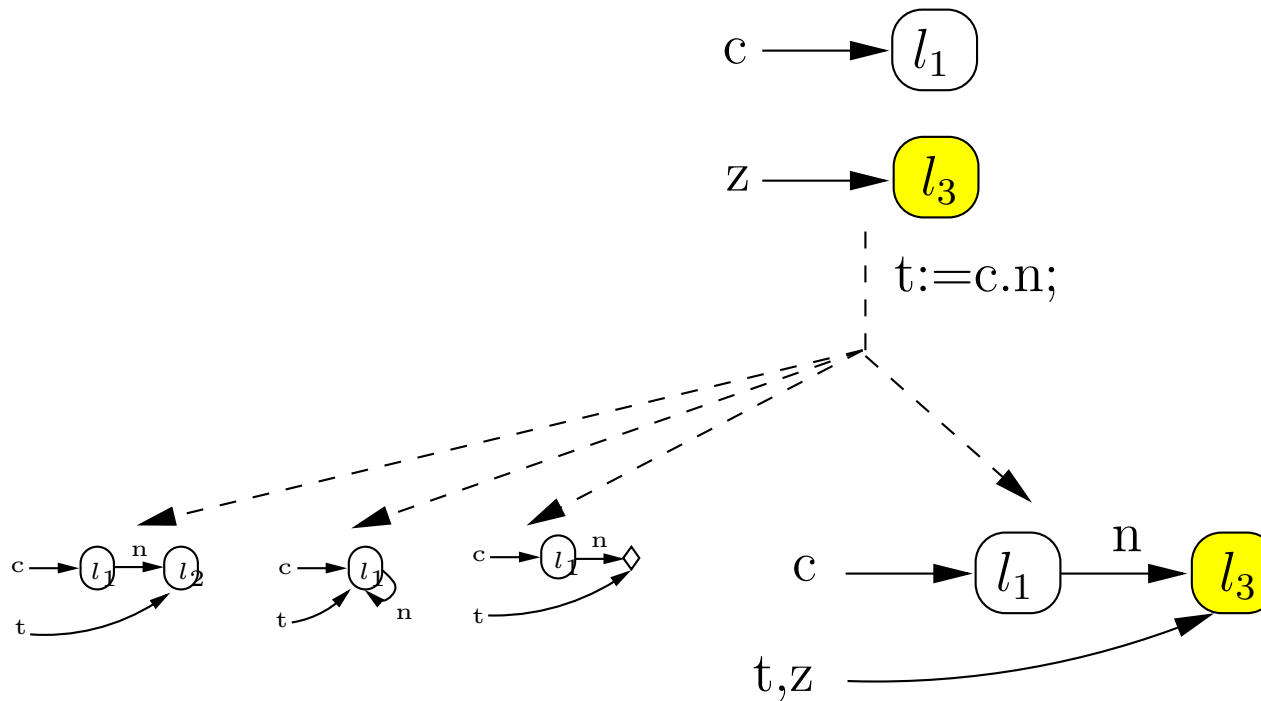
Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- **Lazy Initialization**
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks



$$type(l_3) \leq type(n)$$

$$age(l_3) \geq age(l_1)$$

# Lazier Initialization [Deng, Lee and Robby, ASE'06]

Introduction

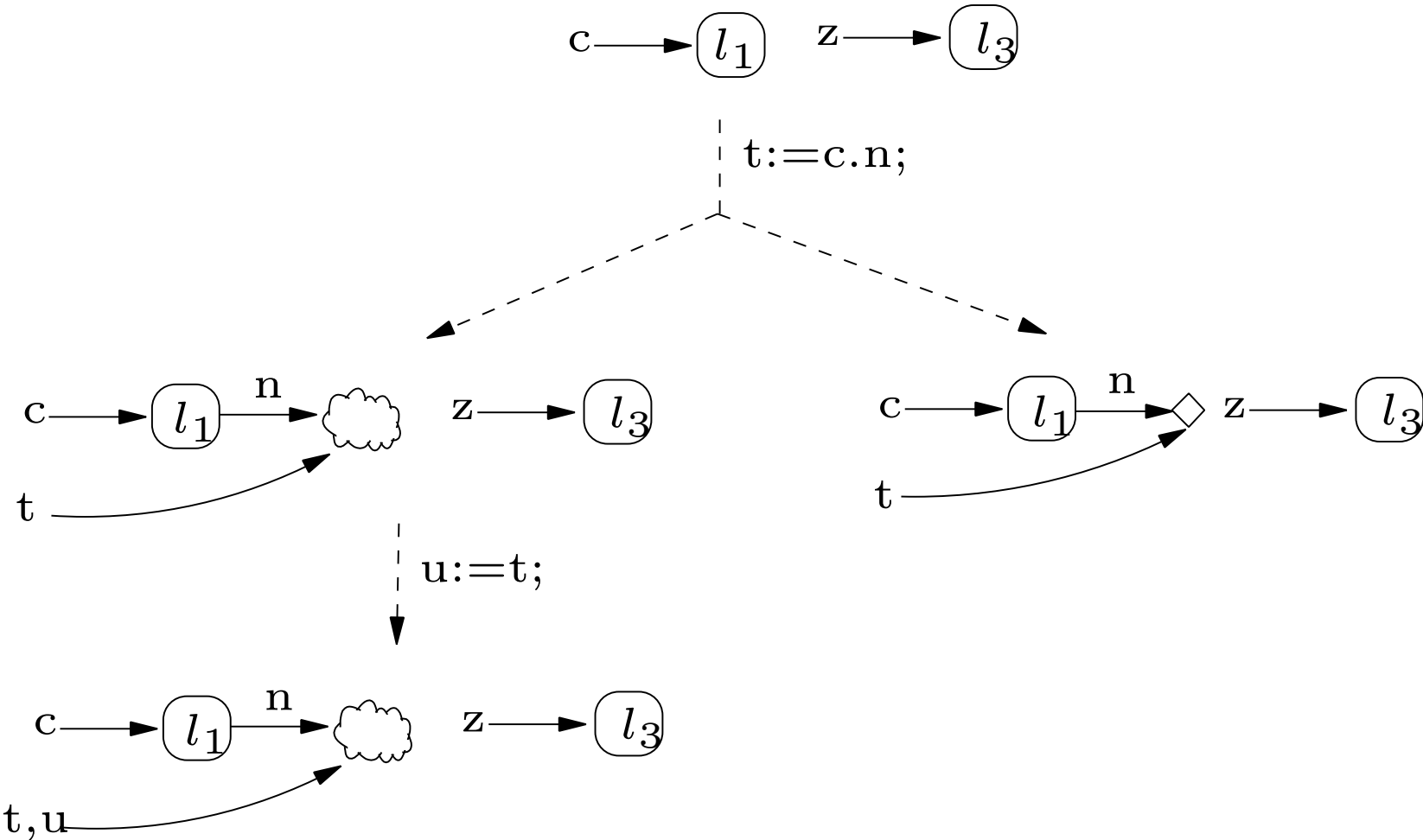
Reverse Execution

Program Validation by Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- **Lazier Initialization**

- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks



# Lazier Initialization [Deng, Lee and Robby, ASE'06]

Introduction

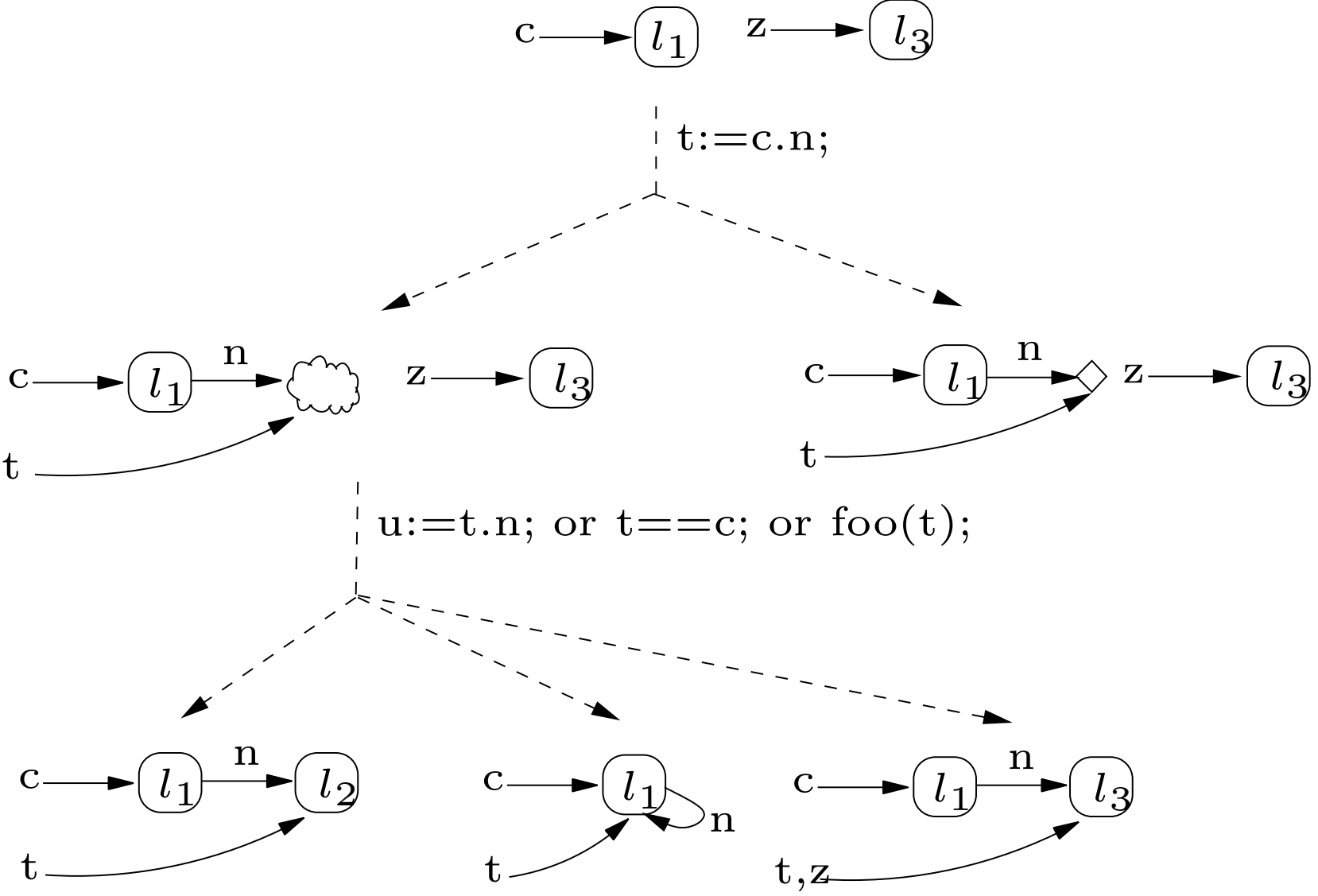
Reverse Execution

Program Validation by Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- **Lazier Initialization**

- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks



# Lazy vs. Lazier

Introduction

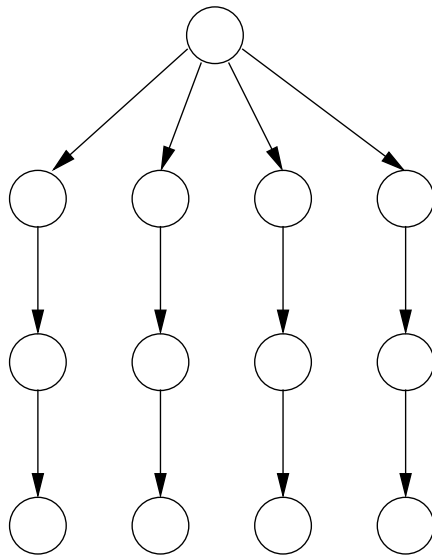
Reverse Execution

Program Validation by  
Symbolic Execution

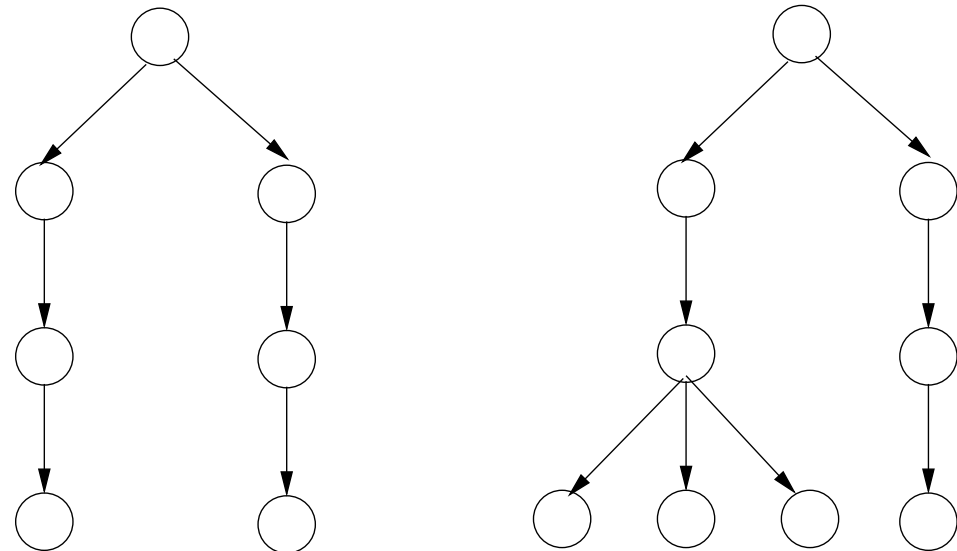
- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- **Lazy vs. Lazier**
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks

## ■ Lazy Initialization



## ■ Lazier Initialization

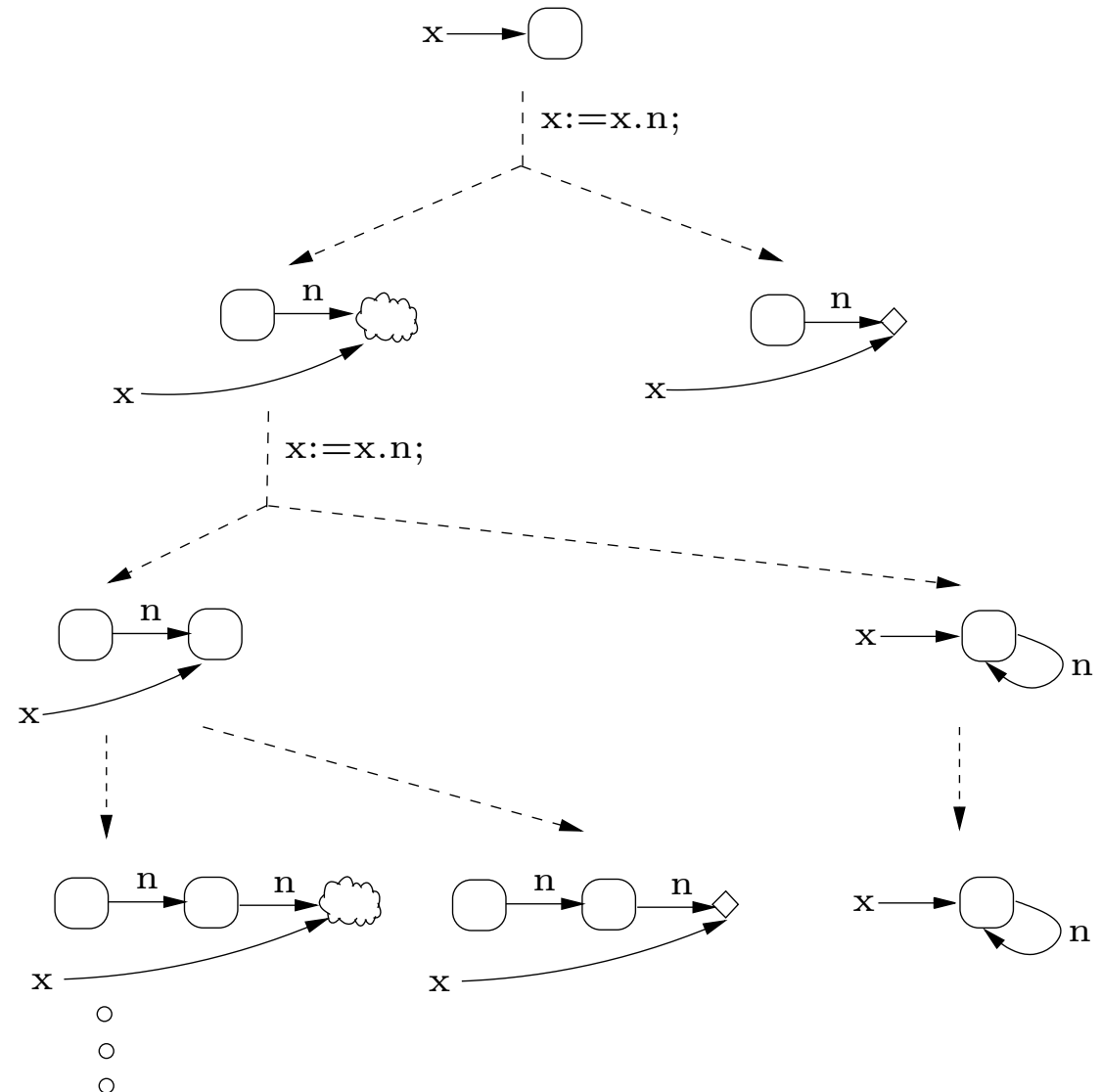


# Loop Example

```

bag.add(x);
while (x ≠ nil) {
  x := x.n;
  if (bag.has(x))
    break;
  else
    bag.add(x);
}

```



Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier

● Loop Example

- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL  
Tree

Concluding Remarks

# Solutions

Introduction

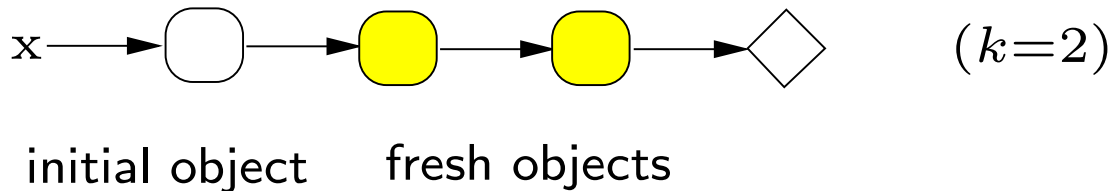
Reverse Execution

Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- **Solutions**
- Bounded Symbolic Execution
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks

- Loop-invariant: heavy annotation
- Abstract interpretation:
  - ◆ automatic verification
  - ◆ false alarm, scalability issue
- Bounding:
  - ◆ no false alarm
  - ◆ suitable at the early phase of validation
  - ◆ easily applicable to any program with a small bound
  - ◆ BMC (transition), Alloy (domain of variables)



# Bounded Symbolic Execution

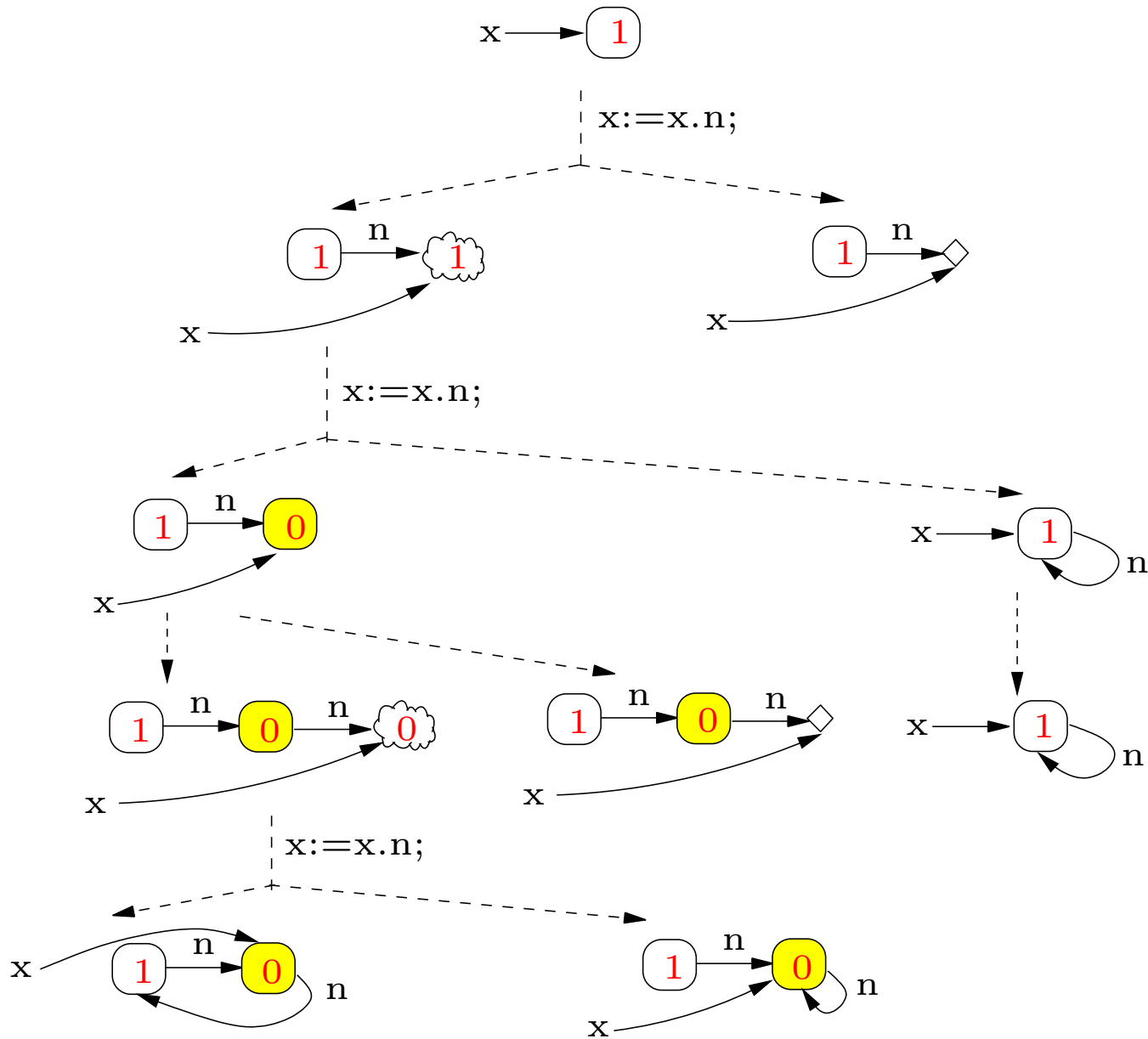
Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- **Bounded Symbolic Execution**
- Soundness
- Completeness
- Insertion Procedure of AVL Tree

Concluding Remarks





# Soundness

Introduction

---

Reverse Execution

---

Program Validation by  
Symbolic Execution

---

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- **Soundness**
- Completeness
- Insertion Procedure of AVL  
Tree

Concluding Remarks

---

If an error is found by our symbolic execution, this error can take place in a concrete execution.

## ■ Assumptions

1. The underlying theorem prover can tell all the infeasible path conditions.
2. Specifications of methods are reliable.

## ■ Proof: by a simulation

# Completeness

Introduction

---

Reverse Execution

---

Program Validation by  
Symbolic Execution

---

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- **Completeness**
- Insertion Procedure of AVL  
Tree

Concluding Remarks

---

If an error can take place in a concrete execution, this error must be able to be found by our symbolic execution.

## ■ Assumptions

1. The length of every possible execution path is finite.
2. A bound in use is sufficiently large.
3. Specifications of methods are precise enough.

## ■ Proof: by a simulation

# Insertion Procedure of AVL Tree

Introduction

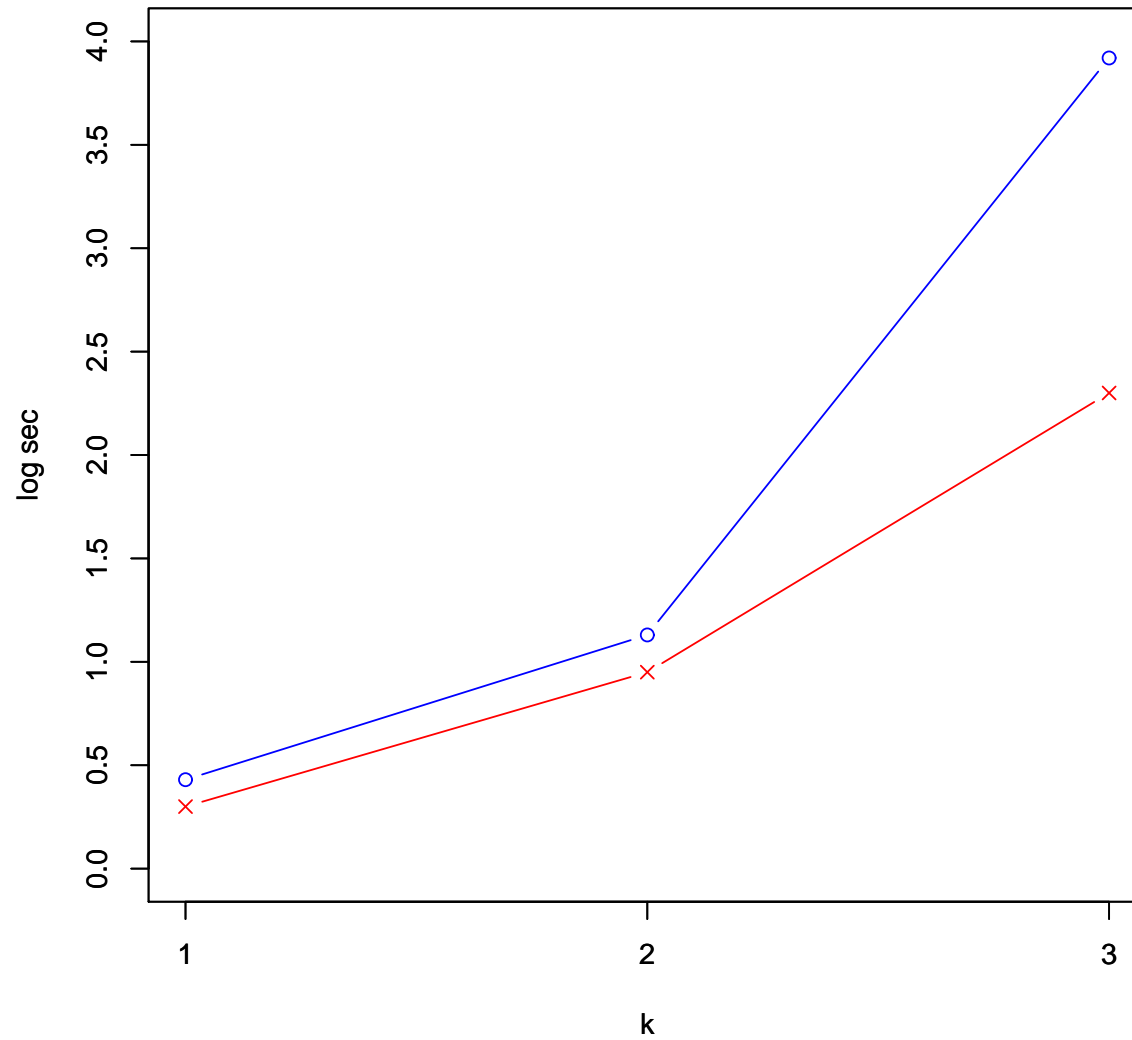
Reverse Execution

Program Validation by  
Symbolic Execution

- Testing
- Symbolic Execution
- Heap
- Symbolic Execution on Heap
- Constraint Solver
- Lazy Initialization
- Lazier Initialization
- Lazy vs. Lazier
- Loop Example
- Solutions
- Bounded Symbolic Execution
- Soundness
- Completeness

● Insertion Procedure of AVL  
Tree

Concluding Remarks



Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

**Concluding Remarks**

- Recap
- Future Work
- Publications

# Concluding Remarks

# Recap

Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

Concluding Remarks

● Recap

● Future Work

● Publications

## ■ Introduction

- ◆ Thesis topic (what): program validation
- ◆ Thesis topic (how): symbolic and reverse execution

## ■ Reverse Execution

- ◆ Reverse execution helps to locate a bug
- ◆ Introduced dynamic reverse code generation (DRCG)
- ◆ DRCG scales to multi-threaded programs
- ◆ DRCG is sound

## ■ Symbolic Execution

- ◆ Symbolic execution helps to check for a bug
- ◆ Introduced bounded lazier initialization (BLI)
- ◆ BLI is useful for finding heap-related bugs
- ◆ BLI is sound in the sense of bug-finding

# Future Work

---

## ■ Reverse Execution

- ◆ Empirical studies focusing on efficient data structures and algorithms
- ◆ Application to other languages of different paradigms
- ◆ Exploration of a programming language suitable for reverse-code generation

## ■ Symbolic Execution

- ◆ Maximum bound inference
- ◆ Loop-invariant inference

# Publications

Introduction

Reverse Execution

Program Validation by  
Symbolic Execution

Concluding Remarks

● Recap

● Future Work

● Publications

- Jooyong Lee.  
Reverse code generation for Java program model checking.  
In *Proceedings of Winter School on Modeling and Verifying Parallel Processes (MOVEP'04)*, pages 89-95, 2004.
- Jooyong Lee.  
Dynamic reverse code generation for backward execution.  
In *Proceedings of the Post-CAV Workshop on Verification and Debugging (V&D'06)*, pages 25-43, 2006.
- Jooyong Lee.  
A case for dynamic reverse-code generation.  
*Submitted.*
- Xianghua Deng, Jooyong Lee and Robby.  
Bogor/Kiasan: A  $k$ -bounded Symbolic Execution for  
Checking Strong Heap Properties of Open Systems.  
In *Proceedings of Conference on Automated Software Engineering (ASE'06)*, pages 157-166, 2006.